Tutorials and Reference Guide



LISA Finite Element Analysis

Software Version 8.0.0 2013

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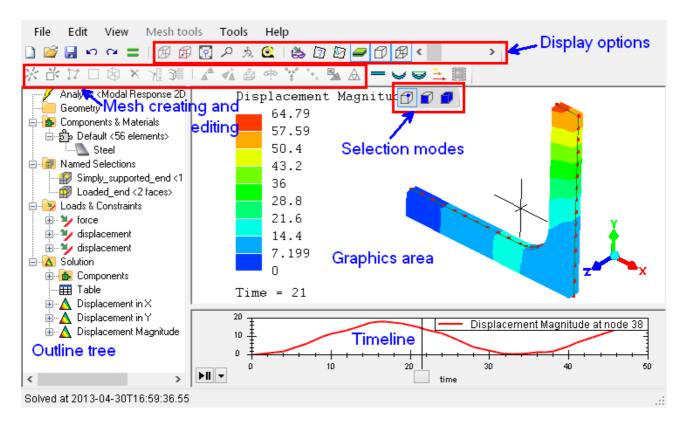
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Overview of LISA

This chapter introduces you to the LISA work-flow for accomplishing your finite element analysis.



1.1 Mesh

A finite element mesh consists of nodes (points) and elements (shapes which link the nodes together). Elements represent material so they should fill the volume of the object being modeled. The mesh is displayed in the graphics area which occupies most of the LISA window.

You can edit a mesh using the **Mesh tools** menu or by selecting parts and using the right-click context menu to access the mesh editing tools.

The other contents of a model are shown in the outline tree on the left hand side of the window. It has several groups containing different types of item listed below. Most of these items can be modified through a context menu which you can access by right-clicking on them.

1.2 Analysis

You can change global properties such as analysis type, physical constants, solver settings and output options by editing the Analysis item in the outline tree

1.3 Geometry

If you generate a mesh from a STEP or IGES file exported from CAD then these files are shown in the Geometry group. Each geometry item can be auto-meshed to generate a mesh.

1.4 Components & Materials

A component is an exclusive collection of elements. Every element must belong to exactly one component. The default component is created automatically and cannot be deleted.

Components are used for assigning materials and controlling the appearance (color and visibility) of elements. All elements in a component share the same material and color. For complex models with logically different parts or features it can be helpful to assign each part to a component to aid in working on the mesh.

Each component containing some elements must have a material assigned to it. The same material can be shared between several components.

You can convert a component to a named selection by selecting its elements then creating a new element selection or adding them to an existing named selection. A named selection containing elements can be converted to a component in a similar way.

1.5 Named Selections

A named selection is a non-exclusive collection of nodes, elements or faces. A face is a face or edge of an element. Named selections are used for applying loads and constraints. For example, to apply a force to the surface of an object, instead of applying a separate for on every face in the surface, you would put all the faces in a named selection and apply a single force to the named selection.

1.6 Loads & Constraints

This group contains all the loads and constraints in the model. It can also contain load cases with their own loads. Loads which are applied to named selections show their named selections as child nodes in the outline tree.

1.7 Solution

After solving, the results are shown under the **Solution** branch in the outline tree. You can click on a field value to display a colored contour plot of it.

Viewing and Selecting

2.1 Zoom, Pan, Rotate

2.1.1 Tool buttons

- Fit to screen
- Use the left mouse button to zoom
- Use the left mouse button to rotate
- Rotate to isometric view
- Rotate to orthogonal view

2.1.2 Keyboard

PgUpZoom-inPgDnZoom-out

Arrow Keys Pan up/down/left/right

Alt + Arrow Keys Rotate

F8 Fit to screen and rotate to isomeric view

2.1.3 Mouse

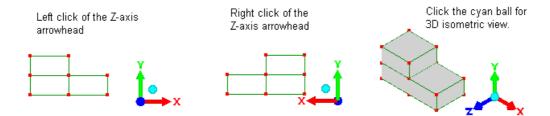
Rotate Drag the cursor with the middle button

Zoom Rotate the mouse wheel

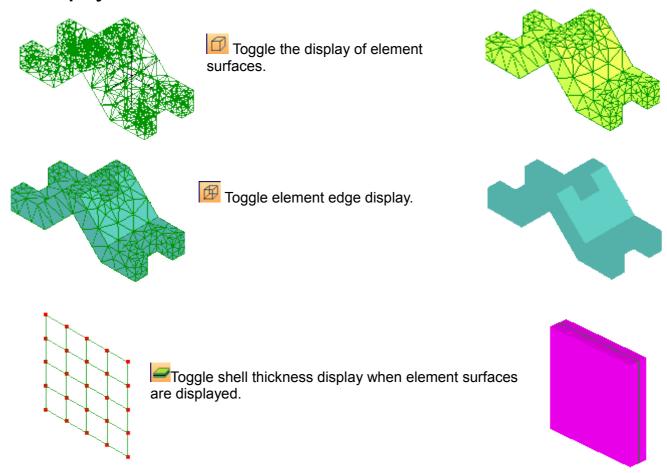
Pan Drag the cursor with the right button

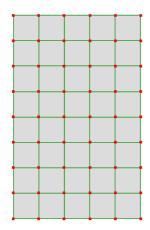
2.1.4 Triad

The triad at the bottom right of the screen can be used to rotate the view parallel to the XY, YZ or ZX planes or isometrically.

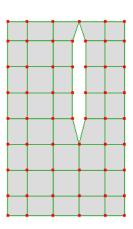


2.2 Display modes



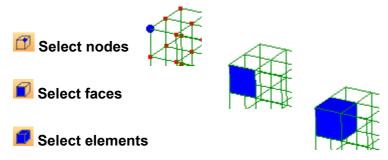


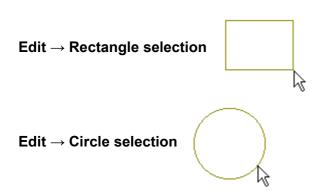
Open cracks in the **View** menu toggles this mode. It helps to show narrow gaps in the mesh where elements appear to be connected but are not sharing the same nodes. When open cracks mode is on, the outside surface of a mesh is shrunk, enlarging any gaps.



2.3 Selection

LISA is selection driven which means to perform most mesh editing tasks you first have to select nodes, element faces or entire elements.





Hold **Ctrl** while selecting to add or remove items from the selection.

Hold the **Shift** key to disable node dragging while selecting nodes with mouse.

2.3.1 Selection tutorial

Step 1

Open SelectionTutorial.liml from the tutorials folder where LISA has been installed.

Step 2

Click the X arrowhead of the triad to switch to side view.



Activate Select nodes



Drag the mouse over the entire mesh.



Rotate the model to observe that all the nodes have been selected even the ones hidden from view.

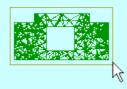
Click in the open space to deselect the model.

Step 3

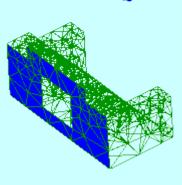
Return to the side view.



Activate **Select faces** and drag the mouse over the entire mesh.

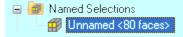


Rotate the model to see that the mesh hidden from view didn't get selected. Keep these faces selected for the next step.

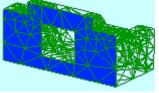


Step 4

This face selection can be saved as a Named Selection which will be shown in the outline tree. Right click a selected face and click Add faces to new named selection



Click an empty space to deselect the faces. Then click the newly created Unnamed<80 faces> named selection to reselect these faces. Right click Unnamed to Rename it.

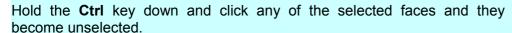


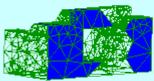
Step 5

To illustrate the effect of the **Ctrl** key, activate **Select faces** and drag to select any section of the mesh. It doesn't need to look like this image.



Hold the **Ctrl** key down and drag to select another area of the mesh. This new selection is added to the faces that were first selected.





Units

LISA doesn't use any system of units itself. You must apply consistent units to all quantities. This table shows 8 examples of consistent unit systems. Four of these are expanded in more detail in the subsequent table.

	SI			MMGS	FPS		IPS	
Length	m	mm	mm	mm	ft	ft	in	in
Mass	kg	kg	Mg	g	slug	Ib _M	lb _{F.} s²/in	Ib _M
Force	N	mN	N	μΝ	lb _F	lb _M .ft/s ²	lb _F	Ib _M .in/s ²
Time	S	s	s	s	s	s	s	s

Note that lb_M (pound-mass) and lb_F (pound-force) are usually not consistent with each other. In the IPS system, density has units of lb_Fs^2/in^4 , not lb_M/in^3 . If you know a density value in terms of lb_M/in^3 , you need to convert it to lb_Fs^2/in^4 by dividing it by standard gravity, $32.174 \times 12in/s^2$. For example if the density is $0.283 \ lb_M/in^3$ you would use $.000733 \ lb_Fs^2/in^4$ in LISA.

		SI m, kg, s, A, K	MMGS mm, g, s	FPS ft, lb _F , s	IPS in, lb _F , s
	Displacement Length	m	mm	ft	in
	Force Moment per length (MomentU, etc.) Shear force	N kg.m/s²	μN g.mm/s²	lb	
S	Mass	kg	g	slug lb.s²/ft	slinch lb.s²/in
Mechanical	Pressure Stress Force per area Young's modulus Shear modulus Shear flexibility Energy density	Pa J/m kg.m g.mm	1 ³ -1 s -2	lb/ft² psi lb/in²	
	Density	kg/m³	g/mm³	slug/ft³ lb.s²/ft⁴	slinch/in ³ lb.s²/in⁴
	Area density	kg/m²	g/mm²	slug/ft² lb.s²/ft³	slinch/in² lb.s²/in³

	Moment	N.m	μN.mm g.mm²/s²	ft.lb	in.lb
	Torsion				
	Shear force per length Force per length Tension per length Spring constant	N/m kg/s²	μN/mm g/s²	lb/ft	lb/in
	Area	m²	mm²	ft²	in ²
	Velocity Speed	m/s	mm/s	ft/s	in/s
	Angular velocity		radiar	n/s	
	Acceleration	m/s ²	mm/s ²	ft/s²	in/s²
	Heat transfer rate	W kg.m²s ⁻³	nW g.mm ² s ⁻³	ft.lb/s	in.lb/s
	Rotational inertia	kg.m²	g.mm²	slug.ft² lb.ft.s²	lb.in.s ²
	Pressure gradient (dP/dX)	Pa/m kg.s ⁻² m ⁻²	Pa/mm g.s ⁻² mm ⁻²	lb/ft³	lb/in³
	Heat flux	W/m² kg.s ⁻³	nW/mm² g.s ⁻³	lb.s ⁻¹ ft ⁻¹	lb.s ⁻¹ in ⁻¹
	Power density Internal heat source	W/m ³ nW/mm ³ kg.s ⁻³ m ⁻¹ g.s ⁻³ mm ⁻¹		lb.s ⁻¹ ft ⁻²	lb.s ⁻¹ in ⁻²
	Flow rate	m ³ /s	mm³/s	ft ³ /s	in ³ /s
	Velocity potential	m²/s	mm²/s	ft²/s	in²/s
	Vorticity	76	s ⁻¹		
	Dynamic viscosity	Pa kg.m g.mn	- ⁻¹ s- ⁻¹ 1 ⁻¹ s ⁻¹	slug.ft ⁻¹ s ⁻¹ lb.s/ft ²	lb.s/in²
	Consistency index K	Pa.s ⁿ Ns ⁿ /m ² kg.s ⁿ⁻² m ⁻¹ g.s ⁿ⁻² mm ⁻¹		lb.s ⁿ /ft²	lb.s ⁿ /in ²
	Temperature	K	K	°R	°R
	Heat transfer coefficient	W.m ⁻² K ⁻¹ kg.s ⁻³ K ⁻¹	nW.mm ⁻² K ⁻¹ g.s ⁻³ K ⁻¹	lb.s ⁻¹ ft ⁻¹⁰ F ⁻¹	lb.s ⁻¹ in ⁻¹⁰ F ⁻¹
	Stefan-Boltzmann constant	Wm ⁻² K ⁻⁴ kg.s ⁻³ K ⁻⁴	nW.mm ⁻² K ⁻⁴	n/a	n/a
	Thermal expansion coefficient	K.	1	°F ⁻¹	°F ⁻¹
	Thermal conductivity	W.m ⁻¹ K ⁻¹ kg.m.s ⁻³ K ⁻¹	nW.mm ⁻¹ K ⁻¹	lb.s ⁻¹⁰ F ⁻¹	lb.s ⁻¹⁰ F ⁻¹
	Specific heat	J.kg ⁻¹ K ⁻¹ m ² K ⁻¹ s ⁻²	nJ.g ⁻¹ K ⁻¹	ft²s-²ºF -1	in ² s ⁻²⁰ F ⁻¹
Ē	Voltage	V m²kg.s ⁻³ A ⁻¹	nV mm²g.s ⁻³ A ⁻¹		
ect ₁	Electric current	Α			
Electromagnetic	Electric charge	C A.s			
gn€	Current density	A/m ²	A/mm ²		
tic	Electric field	V/m	nV/mm		
1		m.kg.s ⁻³ A ⁻¹	mm.g.s ⁻³ A ⁻¹		

Electric flux density	C/m² A.s/m²	C/mm² A.s/mm²		
Magnetic potential Magnetic flux lines	Wb/m m.kg.s ⁻² A ⁻¹	nV.s/mm mm.g.s ⁻² A ⁻¹		
Magnetic flux density B	T kg.s ⁻² A ⁻¹	mT g.s ⁻² A ⁻¹		
Magnetic field intensity H	A/m	A/mm		
Absolute permittivity	F/m m⁻³kg⁻¹s⁴A²	GF/mm mm ⁻³ g ⁻¹ s ⁴ A ²		
Absolute permeability	H/m m.kg.s ⁻² A ⁻²	nH/mm mm.g.s ⁻² A ⁻²		
Electrical conductivity	S/m m ⁻³ kg ⁻¹ s ³ A ²	GS/mm mm ⁻³ g ⁻¹ s ³ A ²		
Resistance	Ω m 2 kg.s $^{-3}$ A $^{-2}$	$n\Omega$ mm ² g.s ⁻³ A ⁻²		
Node rotational DOF angle		radia	n	
Node transform angle Angle for principal stress	dimensionless			
Height gradient (dZ/dX) Emissivity Poisson ratio Flow behavior index n				

Mesh Creation

4.1 Manual meshing

LISA supplies tools for creating models without the use of a CAD file.

4.1.1 Essential tools

The following tools can be used for manual meshing.

a. Quick square / Quick cube

To test a LISA feature you will often create a quick shell or solid element with unit dimensions.

Mesh tools → Create → Quick square and

Mesh tools → Create → Quick cube

b. Create a node



c. Create an element

Use **Mesh tools** → **Create** → **Element...** or if to create an element either by selecting the nodes using the mouse or entering a list of node numbers. Don't select the nodes haphazardly, but follow the number sequence shown in the diagram on the dialog box.

d. Create a circle / arc

Use **Mesh tools** → **Create** → **Curve generator...** Center and start point arc for arc. The Center and start point arc requires an angle less than 180°. For a 180° or greater arc use the Three point arc Three point arc

e. Create a line

Use the Mesh tools → Create → Curve generator... \ Straight line or create the end nodes and then create a single element over that length, then use the refine tool to convert it into multiple elements.

f. Create a curve defined by equations

Use the **Mesh tools** \rightarrow **Create** \rightarrow **Curve generator...** and enter parametric equations for X, Y and Z in terms of the parameter p. Specify the interval for p and the number of elements to create.

g. Move

Mesh tools \rightarrow **Move/Copy...** to translate elements or nodes. It can create a copy of the original mesh or just move it.

h. Rotate

Mesh tools → **Rotate/Copy...** to rotate elements or nodes. It can create a copy of the original mesh or just move it.

i. Mirror

Mesh tools → **Mirror/Copy...** to mirror elements or nodes about the XY, YZ or ZX planes, or about a point defined by a node's location. It can create a copy of the original mesh or just move it.

i. Eliminating duplicate nodes

Duplicate nodes are often a by-product of meshing operations and need to be removed. Use **Mesh tools** \rightarrow **Merge nearby nodes...**, type in a small radius within which the duplicate nodes are to be replaced by a singe node. Too small a value may not eliminate all duplicates and too large a value will collapse elements (if two or more nodes of the same element are replaced by a single node, the element collapses). Start with a very small value such as 0.00001 and use the **View** \rightarrow **Open cracks** to check if gaps are still present.

If some nodes are selected before using this tool then only the selected nodes will be considered. However if you check **Merge other nodes into selected nodes** then the selected nodes will not be moved but any other nodes within the tolerance distance will be merged with them.

k. Eliminating unused nodes

Deleted elements may leave behind nodes. Any that are not re-used should be eliminated using **Mesh** tools \rightarrow Delete unused nodes.

I. Deleting items

To delete elements, first select them or any of their faces then press **Del**. This will also delete any unused nodes left behind. To delete elements without deleting their nodes press **Ctrl + Del**.

To delete a component along with all its elements and their nodes, right click the component in the outline tree and select **Delete**.

To delete nodes, first select the nodes then press **Del**.

4.1.2 Essential tools tutorial

Step 1

Mesh tools → Create → Curve generator... Center and start point arc

Center 0,0,0 **Start Point** 5,0,0

End Point 0,5,0

Step 2

Mesh tools \rightarrow Create \rightarrow Curve generator...

6

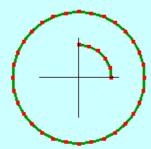


Number of Nodes

D1 20

D2 20

0 X

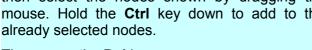


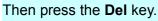
Step 3

Activate the Select nodes mode



then select the nodes shown by dragging the mouse. Hold the Ctrl key down to add to the already selected nodes.



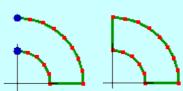




Select Mesh tools → Create → Element... or click if and choose line2 beam/truss

Click these two nodes

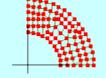
next click these nodes



Step 5

Mesh tools → Automesh 2D...

Maximum element size



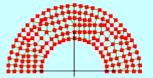
Step 6

Drag and select all the nodes



Mesh tools → Rotate/Copy...

Rotation about point 0,0,0 Specify rotation angles around X,Y,Z axis in degrees 0,0,90



Check Copy

In this particular illustration the nodal patterns at the mating edge do line up, however, it will not always be so with meshes generated by the automesher. The automesher should be used to create an entire mesh rather than a section for duplicating to build up the rest of the mesh.

Step 7

Drag and select all the nodes



Mesh tools → Mirror/Copy...

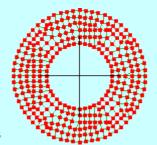
Mirror plane ZX plane

Check Copy

Step 8

View → Open cracks

The gaps mean that the mesh is not continuous.

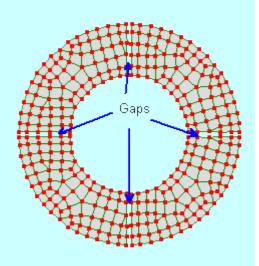


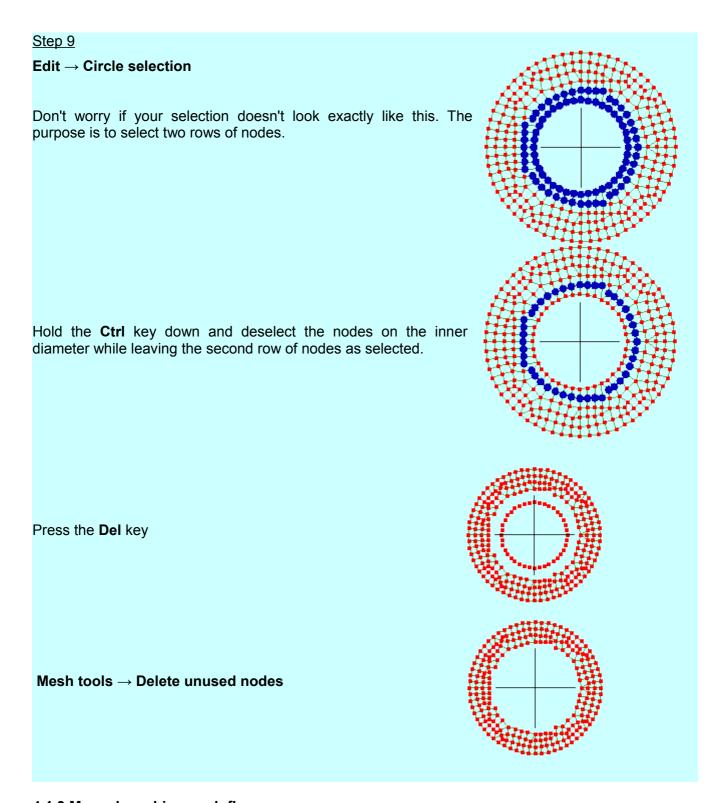
$\textbf{Mesh tools} \rightarrow \textbf{Merge nearby nodes...}$

Distance tolerance 0.00001

View → Open cracks

It's now a continuous mesh.

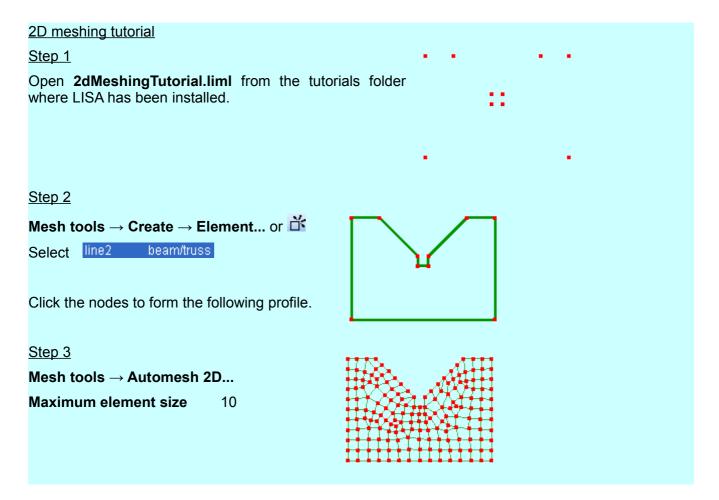




4.1.3 Manual meshing work-flow

Use 2 node line elements to lay out the boundary of a 2D planar area and any holes. The 2D automesher will mesh everything including the holes, so the elements within the holes will need to be

deleted afterwards. The reason it fills holes is so that shaped areas can be extruded or revolved to create 3D meshes.

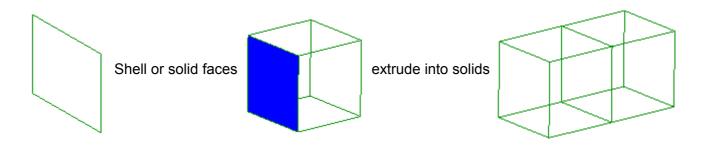


4.1.4 3D manual meshing

Once a 2D plane mesh has been created it can be extruded, revolved or lofted to create a 3D model.

4.1.5 Extrude

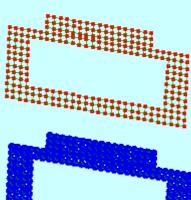
Extrusions can only be done on faces. Select faces using **Select faces**Line elements and shell edge faces extrude into shells



Extrude tutorial

Step 1

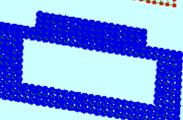
Open ExtrudeTutorial.liml from the tutorials folder where LISA has been installed.



Step 2

Activate **Select faces**



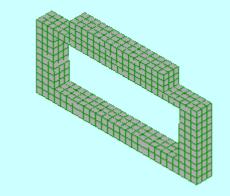


Step 3

Mesh tools → Extrude...

Thickness 5 **Number of subdivisions** 3

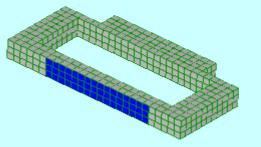
Direction +Z



Step 4

The extrusion step turned off Select faces so reactivate it again.

Select the faces at the bottom.

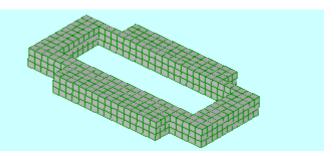


Mesh tools → Extrude...

Thickness 5

Number of subdivisions 3

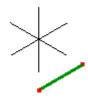
Direction +Normal



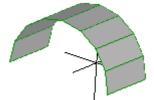
4.1.6 Revolve

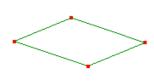
Revolve can only be used on faces. Select faces using Select faces 🗐





Line elements and shell edge faces revolve into shells

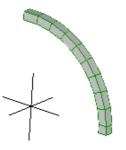




Shell or solid faces



revolve into solids



Revolve tutorial

Step 1

Open RevolveTutorial.liml from the tutorials folder where LISA has been installed.

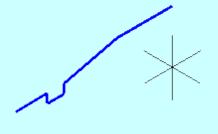


Step 2

Activate Select faces

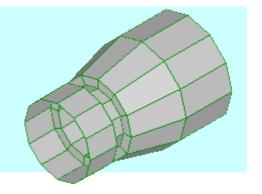


Drag the mouse over the entire mesh so that it becomes selected.



Mesh tools → Revolve...

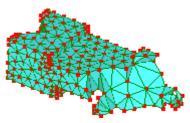
Angle 360
Number of subdivisions 12
Axis of revolution +Z



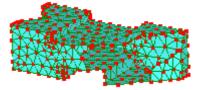
4.1.7 Hollow

The hollow tool will convert a solid mesh into shells. If no elements or nodes are selected then it will use the entire mesh.

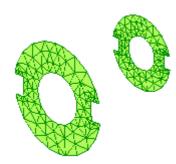
Sectional view showing solid elements.



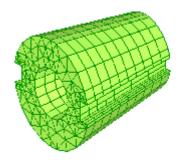
Sectional view after using the hollow tool.



4.1.8 Loft



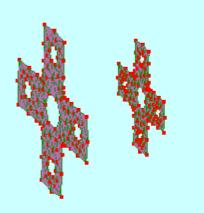
The loft tool fills the gap between two profiles having matching nodal patterns with solid elements. This can used for creating tapered parts. The order of the node numbers must be identical on each profile with the only difference being a constant offset.



Loft tutorial

Step 1

Open LoftTutorial.liml from the tutorials folder where LISA has been installed.



Step 2

Display node and element numbers.



Note down the node numbers of any two corresponding nodes on each profile. In this example the bottom corner node numbers are 12 and 135.



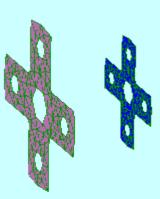


Step 3

Activate Select faces.



Drag to select the profile of node number 135.



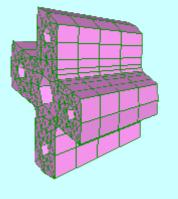
Step 4

Mesh tools → Loft...

Number of subdivisions 4

A node in selected faces 135

The corresponding node 12



4.1.9 Changing element shapes

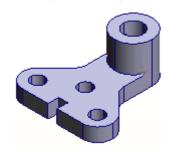


Elements with mid-side nodes converge faster.

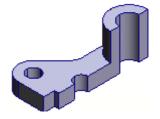


Mesh tools → Change element shapes...

4.2 Symmetry



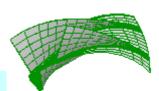
If the geometry, loads & constraints are symmetric (*mirror symmetry*), a model size can be reduced to half or quarter.



When taking advantage of *mirror symmetry* you must enforce constraints at the plane of symmetry. In static analysis the nodes in the plane of symmetry must be constrained so that they do not move out of that plane otherwise a gap or penetration will occur which in reality is not present in the full model. For elements with rotational degrees of freedom like shells and beams, each node that lies in the plane of symmetry should be constrained to have no rotation about either of the two axes that also lie in the plane of symmetry. In thermal analysis there should be no heat flow across a plane of symmetry, which is a condition that is automatically enforced where no other boundary conditions are specified. The same concept extends to fluid, magnetostatic, DC current flow and electrostatic analyses.

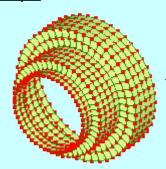
Take care when assuming mirror symmetry for modal vibration or buckling problems because non-symmetric modes will be missed.

Cyclic symmetry which occurs in turbines, fans, etc can be taken advantage of by modeling only a segment containing the cyclic feature rather than the whole wheel. The node patterns must match on both sides of the segment.



4.2.1 Mirror symmetry tutorial

Step 1



This revolved shell can be modeled as only one quadrant.

Open MirrorSymmetryTutorial.liml from the tutorials folder where LISA has been installed.

Step 2

The quarter segment's vertical plane of symmetry is the XY plane and its horizontal plane of symmetry is the ZX plane. Its axis of revolution is the X-axis.

Activate Select nodes

Select the nodes lying in the vertical plane of symmetry. Constraints need to be applied to keep these nodes from moving out of the XY plane, while allowing them the freedom to move within the XY plane.

Right click the selected nodes

Loads & constraints → New displacement

Axis X

Value 0

Since shell nodes have rotational degrees of freedom, the nodes in the XY plane must be prevented from rotating about the X and Y axes.

Right click on the selected nodes again

Loads & constraints → **On Selected Nodes** → **New rotx**

Value 0

Repeat for roty.

Step 3

While still in **Select nodes** mode, select the nodes lying in the horizontal plane of symmetry. Constraints need to be applied to keep these nodes from moving out of the ZX plane or rotating about any axis lying in that plane.

Right click on the selected nodes

Loads & constraints → **New displacement**

Axis X

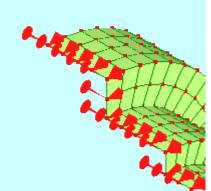
Value 0

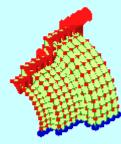
Right click on the selected nodes again

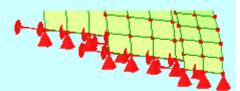
Loads & constraints → **On Selected Nodes** → **New rotx**

Value 0

Repeat for rotz.





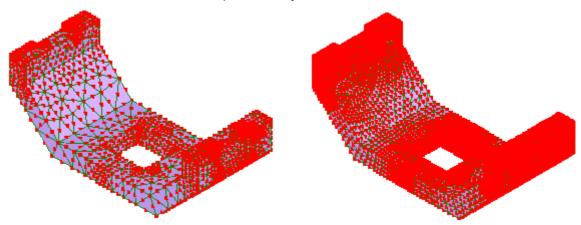


4.3 Mesh refinement

Finite element meshes need to be refined until the results no longer change by more than a small percentage value, at which point the results are said to have **converged** and no advantage would be gained by any further mesh refinement.

4.3.1 Refine all

Mesh tools \rightarrow **Refine** \rightarrow **x2** or \triangle will replace every element in a model with smaller elements.



Or, to replace an existing mesh with a new mesh with controlled element size and local refinement, use **Mesh tools** \rightarrow **Automesh 3D** for 3D meshes or **Mesh tools** \rightarrow **Automesh 2D** for 2D meshes that lie in the X-Y plane.

4.3.2 Refine local 2D & shell

The Mesh tools \rightarrow Refine \rightarrow Quad local refinement x2 and Mesh tools \rightarrow Refine \rightarrow Quad local refinement x3 are used in the same way, the only difference being that x2 is a coarser refinement than x3. The limitation to using this command is that the elements must be 4 node quadrilaterals (quad4) and not triangles.

If the bounding area for refinement includes triangles, the quadrilaterals around the triangles will be refined but not the triangles. This will lead to the mesh error of refined nodes lying on an element edge instead of being connected node-to-node. A node on element edge is no connection at all. One option could be to use the **Mesh tools** \rightarrow **Change element shape...** to first convert all the quadrilaterals into triangles and then repeat this command to convert all the triangles to quadrilaterals. A drawback of this procedure is that the quadrilateral shapes will be severely distorted.

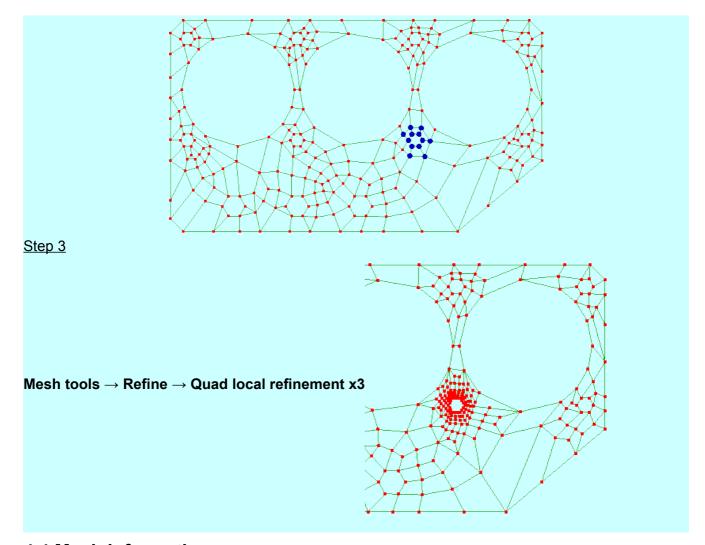
Refine local 2D & shell tutorial

Step 1

Open RefineLocal2dTutorial.liml from the tutorials folder where LISA has been installed.

Step 2

Drag the mouse to select the nodes shown below. Don't worry if you selected a few extra nodes, this is only an illustration.



4.4 Mesh information

4.4.1 Volume

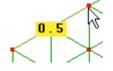
 $\textbf{Tools} \rightarrow \textbf{Volume}$ will report the volume of selected elements. If no elements are selected, it will report the full mesh volume.

4.4.2 Surface area

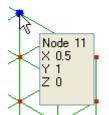
Tools \rightarrow **Surface area** reports the area of selected faces.

4.4.3 Length

Activate the tape measure tool, click and drag from one node to another.



4.4.4 Nodal co-ordinates

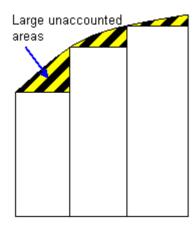


Click a node for a readout of its co-ordinates.

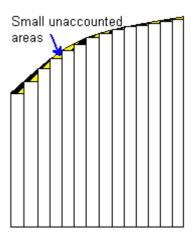
4.5 Modeling errors

Results can only be as accurate as your model. Use rough estimates from hand calculations, experiment or experience to check whether or not the results are reasonable. If the results are not as expected, your model may have serious errors which need to be identified.

4.5.1 Too coarse a mesh

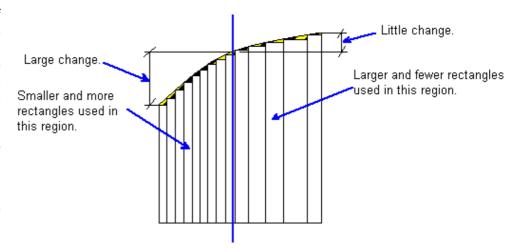


To illustrate the effect of mesh refinement on accuracy, consider the case of finding the area under a curve by the summation of rectangular areas contained within the curve. Clearly, the narrower the rectangles, the more accurate will be the result.



efficient An way refining a mesh is to concentrate the mesh refinement in those areas where the can be accuracy improved, while leaving unchanged those areas that are already accurate.

You will have to run at least one model to identify the areas where the values are changing



a lot and the areas where values are remaining more or less the same. The second run will be your refined model.

Refine areas that see large changes in value. Do not refine areas where values are more or less the same; it will only bloat the size of the model.

4.5.2 Wrong choice of elements

Bending problems with plate-like geometries such as walls, where the thickness is less in comparison to its other dimensions, should be modeled with either shell elements or quadratic solid elements like the 20 node hexahedron or the 10 node tetrahedron. Shell, beam and membrane elements should not be used where their simplified assumptions do not apply. For example beams that are too thick, membranes that are too thick for plane stress and too thin for plane strain, or shells that are initially twisted out of their plane. In each of these cases solid elements should be used.

4.5.3 Linear elements

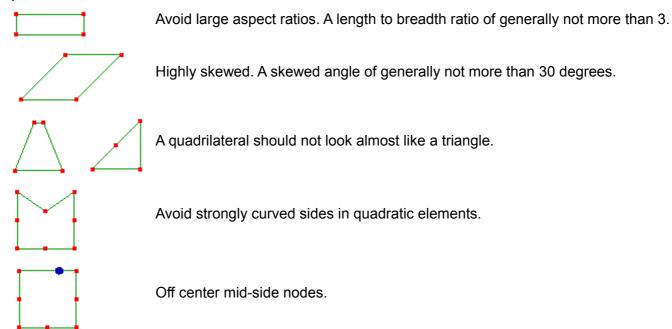


Linear elements (elements with no mid-side nodes) are too stiff in bending so they typically have to be refined more than quadratic elements (elements with mid-side nodes) for results to converge.



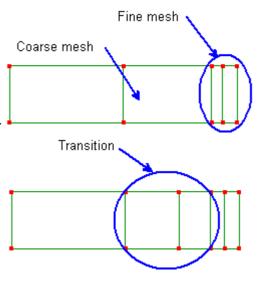
4.5.4 Severely distorted elements

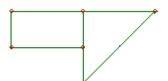
Element shapes that are compact and regular give the greatest accuracy. The ideal triangle is equilateral, the ideal quadrilateral is square, the ideal hexahedron is a cube of equal side length, etc. Distortions tend to reduce accuracy by making the element stiffer than it would be otherwise, usually degrading stresses more than displacements. All the elements in the LISA element library are isoparametric, where a parametric coordinate system is used along the form of the element. Thus, slight to moderate distortions do not have an appreciable effect on the accuracy of the elements. The reality is that shape distortions will occur in FE modeling because it is quite impossible to represent structural geometry with perfectly shaped elements. Any deterioration in accuracy will only be in the vicinity of the badly shaped elements and will not propagate through the model (St. Venant's principle). These artificial disturbances in the field values should not be erroneously accepted as actually being present.



4.5.5 Mesh discontinuities

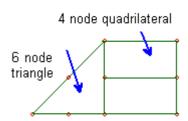
Element sizes should not change abruptly from fine to coarse. Rather they should make the transition gradually.

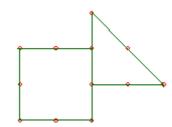




Nodes cannot be connected to element edges. Such arrangements will result in gaps and penetrations that do not occur in reality.

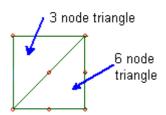
Linear elements (no mid-side node) should not be connected to the midside nodes of quadratic elements, because the edge of the quadratic element deforms quadratically whereas the edges of the linear element deform linearly.





Corner nodes of quadratic elements should not be connected to mid-side nodes. Although both edges deform quadratically, they are not deflecting in sync with each other.

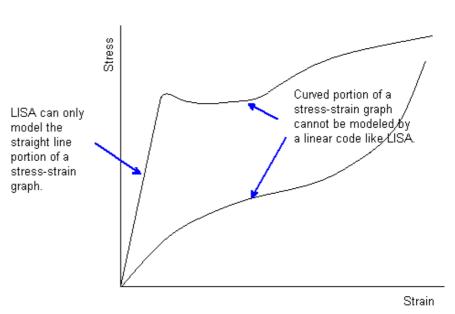
Avoid using linear elements with quadratic elements as the mid side node will open a gap or penetrate the linear element.



None of these is a fatal error. Each will simply cause discontinuities in the results which should not be mistaken as being present in the actual part. These effects will be localized and not propagate through the mesh.

4.5.6 Non-linearities

LISA can model only the linear portion of the stress-strain curve. Another kind of non-linearity which LISA cannot model is large deformations where the stiffness or load changes with deformation.



Shell elements under bending loads should not deform by more than half their thickness otherwise non-linear membrane action occurs in the real world to resist further bending. LISA cannot model resistance due to membrane action.

4.5.7 Improper constraints

Fixed supports will result in less deformation that simple supports which permit material to move within the plane of support.

4.5.8 Rigid body motion

In static analysis, for a structure to be stressed all rigid body motion must be eliminated. For 2D problems there are two translational (along the X- & Y-axes) and one rotational (about the Z-axis) rigid body motions. For 3D problems there are three translational (along the X-, Y- & Z-axes) and three rotational (about the X-,Y- & Z-axes) rigid body motions.

Rigid body motion can be eliminated by applying constraints such as **fixed support**, **displacement** and **rotx**, **roty** and **rotz**.

Modal vibration, dynamic response and modal vibration do not need to have all their rigid body motions eliminated. However the first few modes would be rigid body modes. For example, if you don't apply any constraints in a 3D modal vibration problem then the first 6 modes would be for the 6 rigid body motions. The 7th mode onwards would be the structure's deformation modes.

CAD Models

5.1 Introduction

LISA can open STEP and IGES files which can be output by most CAD applications. It doesn't display the parts but can generate a mesh of them (automesh). Links to CAD models appear in the **Geometry** group in the outline tree. Each geometry item in this group must contain a single solid body so you cannot use assemblies.

IGES files usually have disconnected edges and cannot give a continuous auto-meshed model. Also, LISA cannot generate a volume mesh from an IGES file, so only the **Surface mesh** option is enabled in the **Mesh parameters** dialog box.

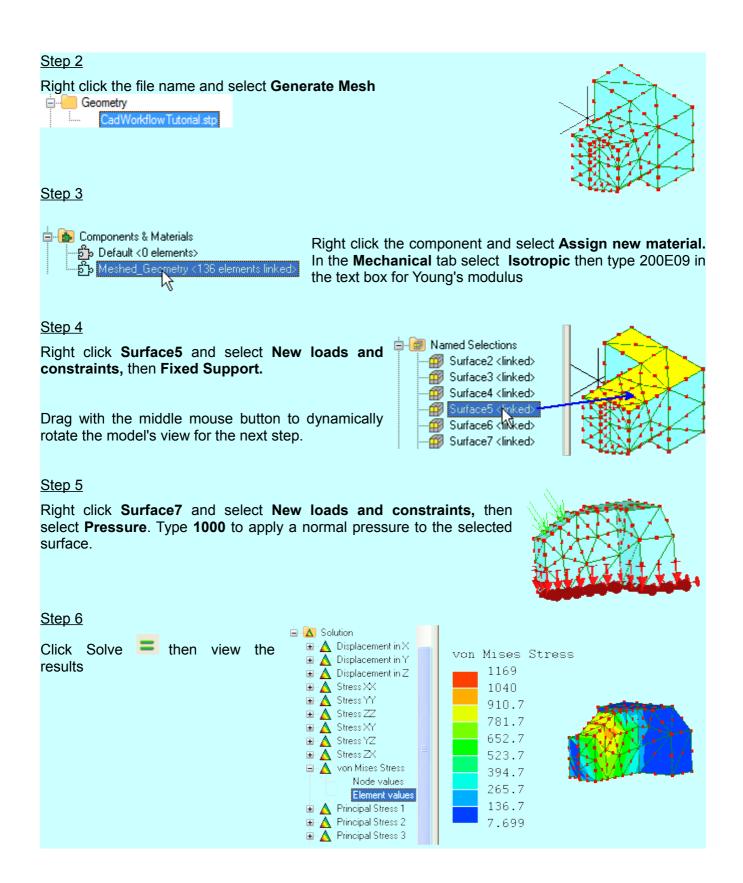
STL (stereolithography) format files can also be opened and saved by LISA. An STL file only contains a set of triangles so these are imported as tri3 elements in LISA without any auto-meshing. Typically, STL files generated by CAD applications contain highly distorted elements so you should use **Automesh 3D** from the **Mesh tools** menu to improve the shape and convert the shells into a solid object.

When you first automesh a geometry item, a component is created for its elements and a named selection is created for each of its surfaces. These named selections are convenient for applying loads and constraints to because they are linked to the geometry item so that it can be auto-meshed again without losing the loads and constraints.

Meshing parameters allow local or global refinement by limiting the maximum element size within spherical regions or over the whole geometry. The size gradient of elements can also be controlled. An aggressive size gradient means each element can be much larger or smaller than its immediate neighbors leading to a low mesh density in large featureless regions and a high density near small details. A gradual size gradient means each element must be a similar size to its immediate neighbors.

To generate a shell mesh, use a solid body as the geometry and set the **Surface mesh** option. This will produce shell elements in the shape of the solid body's surface.

5.1.1 CAD Work-flow tutorial Step 1 Use File → Open or right click Geometry and select Import STEP/IGES files Open the file CadWorkflowTutorial.stp from the tutorials folder where LISA has been installed



5.2 Automeshed CAD models default to millimeters

The automesher converts all CAD model dimensions to millimeters:

- 1. 1mm will remain 1mm
- 2. 1cm will become 10mm
- 3. 1m will become 1000mm
- 4. 1inch will become 25.4mm
- 5. 1foot will become 304.8mm

You have to use the **Mesh tools** → **Scale...** to restore it to the units of the CAD file.

5.2.1 Inch CAD tutorial

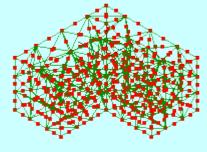
Step 1

Open **InchCadTutorial.stp** from the tutorials folder where LISA has been installed. The overall dimensions of this CAD model are 10"x10"x5".

Step 2

Right click the file name and select Generate Mesh

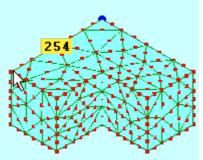




Step 3

Use the tape measure tool-button check the length of the automeshed part. Drag the mouse from one corner node to another.

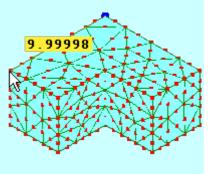
The tape measure readout shows that the length is 254 and not the 10" length of the CAD model.



Step 4

The model will have to be re-sized by 0.03937 (1/25.4). **Mesh tools** \rightarrow **Scale...**, type 0.03937 in the X, Y & Z text-boxes.

Use the tape measure tool to confirm that the edge length is now 10".



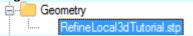
5.3 Local refinement tutorial

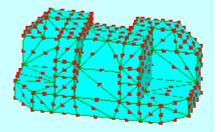
Step 1

Open RefineLocal3dTutorial.stp from the tutorials folder where LISA has been installed.

Step 2

Right click the filename and select Generate mesh



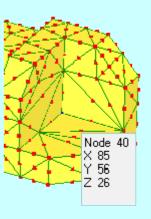


Step 3

We need the co-ordinates of the center of a sphere within which the refinement is to be applied.

Activate Select nodes

Click a node and record the X, Y & Z co-ordinates.



Step 4

Right click the filename and select **New local refinement**

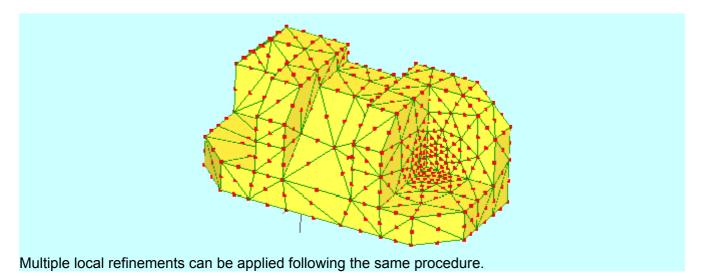


X	85
Υ	56
Z	26
Radius	20
Maximum element size	10

Step 5

Right click the filename and select Generate mesh

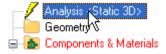




5.4 CAD assemblies

In order for the automesher to operate, the assembly must be a single continuous CAD object. If you combine separate meshes the nodal patterns at the mating surfaces must match in order to be joined correctly into a continuous object. LISA does not have multi-point constraints to connect non-matching nodal patterns at assembly mating surfaces. Consider using beam elements with fictitious high stiffness properties to assemble parts.

Analysis Types



The analysis type determines what physical phenomena are modeled. LISA starts up with Static 3D as the default. Double click **Analysis** or right click it and select **Edit** to switch to another type of analysis such as thermal or modal vibration.

6.1 Static

Static analysis finds the steady state deformation and stress in a structure whose material has a linear stress-strain relationship.

6.1.1 Static 2D

Elements: Plane continuum (tri3, tri6, quad4, quad8, quad9), beam (line2), truss (line2), axial spring (line2)

Loads and constraints: Fixed Support, Displacement, Force, Pressure, Line Pressure, Moment, Gravity, Centrifugal Force, Temperature, Thermal Stress, rotz, nodetemperature, transformrz, mass, Coupled DOF

In Static 2D analysis, all nodes should lie in the XY plane because the Z coordinates are ignored by the solver. Each node has either 2 or 3 DOFs: Nodes of beams have displacement in X, displacement in Y and rotation about Z while nodes of plane, truss and axial spring elements have only the two displacement DOFs.

6.1.2 Static 3D

Elements: Solid continuum (tet4, tet10, pyr5, pyr13, wedge6, wedge15, hex8, hex20), shell (tri6, quad4, quad8, quad9), beam (line2), truss (line2), axial spring (line2)

Loads and constraints: Fixed Support, Displacement, Flexible Joint, Force, Pressure, Line Pressure, Moment, Gravity, Centrifugal Force, Temperature, Thermal Stress, Cyclic Symmetry, rotx, roty, rotz, nodetemperature, transformrx, transformry, transformrz, mass, Coupled DOF

In Static 3D analysis, solid, truss and axial spring elements have 3 DOFs each: displacement in X, Y and Z. Shells and beams have 6 DOFs each: 3 displacements and also rotation about X, Y and Z. You can combine all the different element types in the same model.

6.1.3 Static Axisymmetric

Elements: Axisymmetric continuum (tri3, tri6, quad4, quad8, quad9)

Loads and constraints: Fixed Support, Displacement, Force, Pressure, Line Pressure, Gravity, Centrifugal Force, Temperature, Thermal Stress, nodetemperature, transformrz, mass

Only plane elements can be used here and they will be treated as axisymmetric elements. The Y axis is the axis of symmetry and the X axis is the radial direction. Each node must lie in the two positive X quadrants of the XY plane and have zero Z coordinates.

All nodes have two DOFs: displacement in X and displacement in Y.

6.2 Modal Vibration

Free vibrations of a structure occur due to its own elastic properties when it is disturbed from its equilibrium state. These vibrations only occur at discrete natural frequencies. The two properties required for vibrational motion are:

- elasticity which returns the disturbed structure back to it's equilibrium state, and
- inertia (from the mass) of the structure which makes it overshoot its equilibrium state.

Modal vibration analysis finds the natural frequencies of a structure and the corresponding deflected shapes (mode shapes). This is done without regard to how the vibration was initiated. All the nodes move with simple harmonic motion in phase with one another at the same frequency. Therefore all the time-dependent displacements reach their maximum magnitudes at the same instant of time.

The magnitudes of the displacements and nodal rotations given by LISA are only relative to the other displacements and rotations in the same mode shape. Their absolute magnitude has no meaning.

The maximum number of modes is equal to the number of unconstrained DOF in the model. For example, if a model is a single hex8 element with a fixed support applied to one face, the maximum number of modes will be 12, which is the number of DOFs per node (3) multiplied by the number of unconstrained nodes (4). Unless there is shock loading, only the modes of the lowest frequencies are important in the structural response. The **Default Iterative** matrix solver cannot find the highest one or two modes. If you want to find all the modes then use the **Direct** solver. However this is much slower for models with more than a few hundred nodes.

6.2.1 Modal Vibration 2D Plane and Truss

Elements: Plane continuum (tri3, tri6, quad4, quad8), truss (line2), axial spring (line2)

Loads and constraints: Fixed Support, Displacement, mass

With this analysis type, only two-dimensional truss elements, springs and membrane (plane continuum) elements in plane stress can be used. Membrane elements are appropriate for finding the in-plane vibration modes of a thin sheet while ignoring the out-of-plane modes. Truss and spring elements can be connected to the membrane elements or used on their own.

The model must be made in the XY plane. All Z-coordinates of nodes are ignored by the solver.

6.2.2 Modal Vibration 2D Beam

Elements: Beam (line2)

Loads and constraints: Fixed Support, Displacement, rotz, mass,

rotationalinertiaz

Here only 2D beam elements can be used. The model must be made in the XY plane. All Z-coordinates of nodes are ignored by the solver.

6.2.3 Modal Vibration 3D Solid and Truss

Elements: Solid continuum (tet4, tet10, pyr5, pyr13, wedge6, wedge15, hex8, hex20), truss (line2), axial spring (line2)

Loads and constraints: Fixed Support, Displacement, Force, Pressure, Line Pressure, Gravity, Centrifugal Force, Temperature, Thermal Stress, Cyclic Symmetry, Stress Stiffening, nodetemperature, transformrx, transformry, transformrz, mass

This analysis type is the most generally useful. It can model arbitrary 3D geometries using solid elements as well a truss elements and springs.

The state of stress of a structure can influence its natural frequencies. This effect, called stress stiffening, is particularly apparent in a tensioned cable or guitar string. Static loads can also be applied to use with stress stiffening.

6.2.4 Modal Vibration 3D Shell and Beam

Elements: Shell (quad8), beam (line2)

Loads and constraints: Fixed Support, Displacement, rotx, roty, rotz, mass, rotationalinertiax, rotationalinertiay, rotationalinertiaz

This analysis type is useful for space frames and structures made from thin sheets. Every node has 3 rotational DOF as well as 3 translational DOF, one on each axis.

6.2.5 Modal Vibration 2D Transverse Vibration of Membrane

Elements: Plane continuum (tri3, tri6, quad4, quad8)

Loads and constraints: Fixed Support, Displacement, Tension Per Length

This is a special analysis type for modeling flat sheets of material with negligible bending and shear stiffness but which gain stiffness from their tension. An example is a drumhead. The tension must be uniform over the entire model and is applied using the Tension per length load.

The same structures can typically also be modeled in Modal Vibration 3D Solid and Truss using solid elements with stress stiffening. However that usually requires a finer mesh and it can be difficult to apply loads that lead to uniform tension.

6.3 Modal Response

Modal response has the same function as the dynamic response analysis types - it finds the time dependent deformation of a structure in response to time dependent loads. Modal response uses the mode superposition method which first finds the natural frequencies and mode shapes by solving an eigenvalue problem then generates nodal displacements and rotations at each time step. There are several other differences of modal response from dynamic response in LISA:

- Stresses are not produced.
- It is only suitable for small models, typically less than 1000 nodes, because it finds all modes using the direct matrix solver.
- It can be much faster when a large number of time steps are required.
- Beam elements are available but they cannot be mixed with any other element type.
- Quadratic solid elements (tet10, pyr13, wedge15, hex20) are available.

6.3.1 Modal Response 2D Plane and Truss

Elements: Plane continuum (tri3, tri6, quad4, quad8), truss (line2), axial spring (line2)

Loads and constraints: Fixed Support, Displacement, Force, Pressure, Line Pressure, mass

The model must be made in the XY plane. All Z-coordinates of nodes are ignored by the solver.

6.3.2 Modal Response 2D Beam

Elements: Beam (line2)

Loads and constraints: Fixed Support, Displacement, Force, Pressure, Line Pressure, Moment, rotz, mass, rotationalinertiaz

Here only 2D beam elements can be used. The model must be made in the XY plane. All Z-coordinates of nodes are ignored by the solver.

6.3.3 Modal Response 3D Solid and Truss

Elements: Solid continuum (tet4, tet10, pyr5, pyr13, wedge6, wedge15, hex8, hex20), truss (line2), axial spring (line2)

Loads and constraints: Fixed Support, Displacement, Force, Pressure, Line Pressure, mass

This analysis type can model arbitrary 3D geometries using solid elements as well a truss elements and springs.

6.3.4 Modal Response 3D Beam

Elements: Beam (line2)

Loads and constraints: Fixed Support, Displacement, Force, Pressure, Line Pressure, Moment, rotx, roty, rotz, mass, rotationalinertiax, rotationalinertiay, rotationalinertiaz

This analysis type is useful for space frames. Every node has 3 rotational DOF as well as 3 translational DOF, one on each axis.

6.4 Dynamic Response

When a part or structure is subjected to a time varying load, it's stresses are amplified by an induced vibration. Dynamic response analysis takes this vibration into account when calculating the stresses & strains. It also calculates the velocities & accelerations in the model's response to the vibrating load.

LISA cannot model damping in dynamic response and initial conditions are zero displacement and velocity. You can impose an initial acceleration by applying a load at time zero.

The **Time step** affects the accuracy of the solution with smaller time step sizes being more accurate. You can choose a suitable time step size by first performing a modal vibration analysis to determine the period (1/f) of the highest mode of interest, then starting from that value, repeatedly reduce it and solve the problem again until the solution doesn't change significantly. When you reduce the time step you should also increase the **Number of time steps** by the same proportion to keep the total duration of the analysis unchanged. The total duration of the analysis should be at least the period of the lowest vibration mode. This ensures that all modes oscillate at least once.

Two solution algorithms are available, the **Newmark method** is suitable for most problems and it uses the constant average acceleration assumption which is unconditionally stable. The **Central difference method** typically requires much smaller time steps and may be unstable. The advantage of the central difference method is that each time step requires less CPU time to solve so it can be more efficient in some cases.

Decimation is available to reduce the number of time steps stored in the results. For example, if the model is solving for 1000 time steps you can enter 11 for the **Decimation number of time steps** and it will only output steps 0,100,200, ..., 1000 thereby using 1% of the memory that would be needed for storing all 1001 time steps.

6.4.1 Dynamic Response 2D

Elements: Plane continuum (tri3, tri6, quad4, quad8, quad9), truss (line2), axial spring (line2)

Loads and constraints: Fixed Support, Displacement, Force, Pressure, Line Pressure, Gravity, mass

6.4.2 Dynamic Response 3D

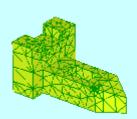
Elements: Solid continuum (tet4, hex8), truss (line2), axial spring (line2)

Loads and constraints: Fixed Support, Displacement, Force, Pressure, Line Pressure, Gravity, mass

Dynamic response tutorial

Step 1

Open **DynamicResponseTutorial.liml** from the tutorials folder where LISA has been installed.



Step 2



Right click **Analysis** and select **Edit**

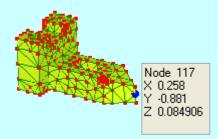
→ General tab

Number of time steps 7

Time step 0.000415

Step 3

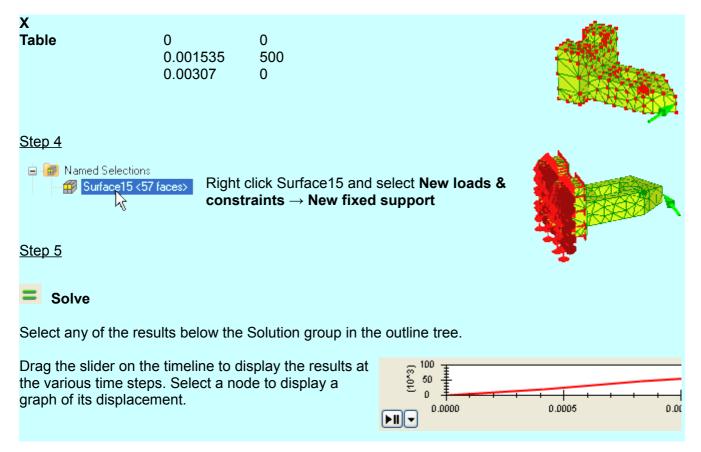
Activate the **Select nodes** mode and select this node.



An applied force will ramp up linearly from 0 to a maximum 500 then down to 0. At each time step LISA will determine the force by interpolating between the specified values.



Right click **Loads & Constraints** and select **New force Named selection**Create from current selection



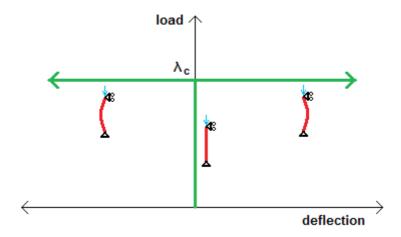
6.4.3 Dynamic Response Axisymmetric

Elements: Axisymmetric continuum (tri3, tri6, quad4, quad8, quad9)

Loads and constraints: Fixed Support, Displacement, Force, Pressure, Line Pressure, Gravity, mass

6.5 Buckling

Linear eigenvalue buckling analysis, such as that provided with LISA, is only capable of describing bifurcation buckling with a constant, symmetric load-deflection relationship as shown below. An Euler column is used as an example, but the same curve can be applied to other structures. Here deflection is the displacement perpendicular to the direction of the load. Symmetric means the structure must be equally able to buckle in two opposite directions. There should also be negligible displacement in any direction prior to buckling.



As the load is increased from 0 to the critical load λc , the structure remains in its original configuration with no deflection. When the load reaches λc , the deflection is indeterminate and increases with no further increase of the load.

Some real structures closely approximate this behaviour, while others are so different that eigenvalue buckling analysis is of no use. You should take care to ensure that these assumptions are appropriate to the problem otherwise the buckling factors may be grossly in error even if the mode shapes are reasonable.

An important class of problems for which eigenvalue buckling analysis is usually unsuitable is limit point instability. Here the structure continuously deflects by a finite amount as load is increased, until a 'limit point' of the load is reached, where it 'snaps through' into a different configuration. An example is a toggle mechanism.

These and other structures which appear to be buckling are in fact general non-linear problems. Another example is a column with an eccentric axial load. The deflection is non-zero for any finite load and there is no bifurcation point.

A thin-walled axially compressed cylinder appears to be a simple problem, but is very sensitive to initial imperfections. Experimental testing shows a wide scatter in critical loads. It also suffers from a range of other difficulties such as closely spaced buckling loads for many different modes, and the formation of plastic hinges on small initial buckles.

Spherical shells subject to uniform external pressure suffer some of the same difficulties as axially compressed cylinders. In both cases eigenvalue buckling analysis is likely to produce very misleading results.

Eigenvalue buckling analysis assumes no imperfections in the material or loading. For this reason the buckling factor is non-conservative and typically underestimates the actual buckling loads.

Each mode has an associated buckling factor. You can think of this as the safety factor. Instability occurs when all the loads are multiplied by the buckling factor. For thermal loads, instability occurs when each node's temperature is

$$T_{cr} = (T_{node} - T_{initial}) \times buckling factor + T_{initial}$$

and any mechanical loads are also scaled by the buckling factor. It can be convenient to specify unit loads in the model so that the buckling factor is equal to the critical load. If some loads are constant,

such as gravity, then you may need to perform several iterations to adjust the unknown loads until the buckling factor becomes 1.

The mode shape represents the relative movement of the nodes immediately after buckling occurs. The actual equilibrium shape of a structure after buckling cannot be found using linear eigenvalue buckling analysis.

To use buckling analysis in LISA you must specify the **Number of modes** and a **Shift point**. The shift point controls the stability of the eigenvalue solver. It must not be zero and should be between zero and the lowest buckling factor. The closer it is to the buckling factors, the greater their accuracy. However modes with buckling factors below the shift point will not be found.

6.5.1 Buckling 2D Beam

Elements: beam (line2)

Loads and constraints: Fixed Support, Displacement, Force, Pressure, Line Pressure, Moment, rotz, mass, rotationalinertiaz

6.5.2 Buckling 3D Solid and Truss

Elements: Solid continuum (tet4, tet10, pyr5, pyr13, wedge6, wedge15, hex8, hex20), truss (line2), axial spring (line2)

Loads and constraints: Fixed Support, Displacement, Force, Pressure, Line Pressure, Gravity, Centrifugal Force, Temperature, Thermal Stress, nodetemperature, transformrx, transformry, transformrz, mass

LISA can model global buckling of a truss structure due to elastic deformation of the individual elements. However it does not consider buckling of individual truss elements. You can calculate these loads from a static analysis using the tensile force values and the Euler column buckling formula.

6.6 Thermal

Thermal analysis uses a single temperature DOF for each node. The solver computes heat flux from the temperature field. All thermal analysis types are 3D. However, you can make a 2D model using shell elements of any thickness laid in a plane.

6.6.1 Thermal Steady State

Elements: Solid continuum (tet4, tet10, pyr5, pyr13, wedge6, wedge15, hex8, hex20), shell (tri3, tri6, quad4, quad8, quad9), fin (line2, line3)

Loads and constraints: Temperature, Heat Flow Rate, Internal Heat Generation, Convection, Radiation, Cyclic Symmetry, nodetemperature, Coupled DOF

This finds the equilibrium temperature distribution in a structure after any transients have dissipated.

6.6.2 Thermal Transient

Elements: Solid continuum (tet4, wedge6, hex8), shell (tri3, tri6, quad4, quad8, quad9), fin (line2, line3)

Loads and constraints: Temperature, Heat Flow Rate, Internal Heat Generation, Convection, Radiation, nodetemperature

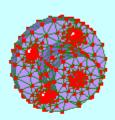
Thermal Transient analysis produces a time history of the temperature field through a structure. You can specify time-dependent loads and temperature constraints as well as an initial temperature distribution. For nodes with no initial temperature specified, LISA applies a default value of zero which may be unrealistic if you are using absolute units such as kelvin.

Decimation is available to reduce the number of time steps stored in the results. For example, if the model is solving for 1000 time steps you can enter 11 for the **Decimation number of time steps** and it will only output steps 0,100,200, ..., 1000 thereby using 1% of the memory that would be needed for storing all 1001 time steps.

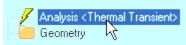
Transient thermal tutorial

Step 1

Open **TransientThermalTutorial.liml** from the tutorials folder where LISA has been installed.



Step 2



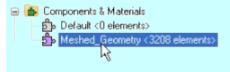
Right click $\mathbf{Analysis}$ and select \mathbf{Edit}

General tab

Number of time steps 30 Time step 10

The duration of the analysis is $30 \times 10s = 300s$ or 5 minutes.

Step 3



Right click Meshed_Geometry and select Assign new material

Mechanical tab

Isotropic

Density 0.0027

Thermal tab

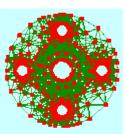
Isotropic

Thermal conductivity 0.204 Specific heat 890

Step 4

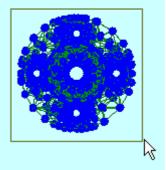


Right click the arrowhead of the Y-axis to display the model parallel to the screen.



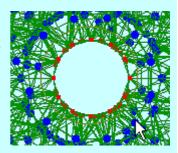
Activate the Select nodes mode.

Drag to select the entire mesh.



Edit → Circle selection

Hold the Ctrl key down and drag to deselect the nodes of the inner diameter.





Right click Initial Conditions and select New temperature

Named selection Create from current selection

Constant

This sets the selected nodes to an initial temperature of 22. The reason the nodes of the inner diameter were deselected is because a constant temperature is going to be applied to the inner diameter. It's not physically possible for a node to be both at an initial temperature of 22 and a different constant temperature at the same time.

Step 5

We will now fix the temperature at the internal diameter to 120 for the entire analysis.



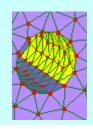
Right click Surface11 and select New loads & constraints

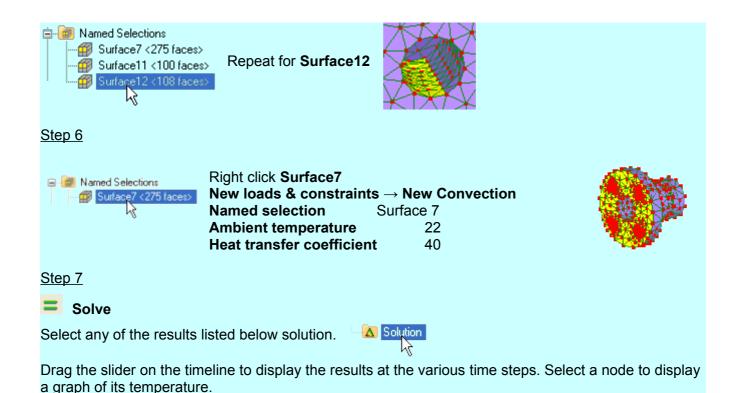
→ New temperature

Surface 11 Named selection

Apply at all times

Constant 120





6.7 Fluid Potential Flow

Potential flow is an idealized fluid flow described by Laplace's equation $\nabla^2 \phi = 0$ where ϕ is the velocity potential. The flow must be incompressible, irrotational and inviscid. Velocity potential is the single degree of freedom used in this analysis type. A gradient in the velocity potential field corresponds to a velocity in a way which is analogous to how a temperature gradient exists with heat flow or an electric potential gradient with current flow.

Three types of boundary condition are available. Where no boundary conditions are specified the default is zero velocity normal to the boundary, which can represent the walls of a container. You can also apply a known flow rate or velocity potential. Fixing the velocity potential on a surface causes the flow to be normal to that surface. At least one node should have a velocity potential defined to ensure stability of the solver.

LISA will calculate velocity and dynamic pressure fields using the following equations:

velocity
$$\mathbf{u} = -\nabla \varphi$$

dynamic pressure = $\rho u^2/2$

To obtain dynamic pressure results, you must specify the fluid's density in the material properties, otherwise density is not required.

6.7.1 Fluid Potential Flow 2D

Elements: Plane continuum (tri3, tri6, quad4, quad8)

Loads and constraints: Flow Rate, velocitypotential

6.7.2 Fluid Potential Flow 3D

Elements: Solid continuum (hex8)

Loads and constraints: Flow Rate, velocitypotential

6.8 Fluid Navier-Stokes Equations

Fluid Navier-Stokes Equations is used to find steady state solutions to the Navier-Stokes equations, which can represent rotational, viscous flow. They are implemented according to [1].

The corner nodes of each element have three degrees of freedom u,p,v:

u = nodal fluid velocity in x-direction

v = nodal fluid velocity in y-direction

p = nodal static pressure.

The midside nodes have only two degrees of freedom, u and v. This means that the velocities are interpolated with quadratic shape functions and pressures are interpolated linearly with the shape functions of tri3 and quad4.

Boundary conditions can be fixed velocities (velx, vely) or fixed pressures (nodepressure). The walls of a vessel should have both velocity components set to zero to prevent flow through the wall and enforce the no-slip condition. Outside faces with no specified boundary conditions are automatically subject to

$$\frac{\partial u}{\partial n} = 0$$
 and $\frac{\partial v}{\partial n} = 0$

where $\frac{\partial}{\partial n}$ is the partial derivative with respect to the face normal. For example a face perpendicular

to the X axis with no other velocity constraints will have $\frac{\partial u}{\partial x} = 0$ and $\frac{\partial v}{\partial x} = 0$

The solver finishes when the relative change in nodal fieldvalues between subsequent iterations falls below the **Convergence tolerance**. Typically 0.01 is adequate.

The solution of each iteration is multiplied by the **Relaxation factor** then used as input to the next iteration. High values such as 1 lead to faster solving but can cause oscillation in some cases. If it fails to converge, reduce this closer to zero.

Approximate nodal velocities can be specified to begin the iteration. They are startvelx and startvely and can be extracted from a previous solution using **Transfer start velocities from solution**. Usually this is unnecessary, but it can help guide unstable problems towards convergence. It can also speed up the solution process.

Many cases where the solver fails or doesn't converge can be caused by its inability to represent unsteady flow which may be caused by turbulence or vortex shedding. Sharp changes in boundary conditions or geometry can lead to such failures. Insufficient constraints on both velocity and pressure can also prevent a solution being found.

6.8.1 Fluid Navier-Stokes Equations 2D

Elements: Plane continuum (tri6, quad8)

Loads and constraints: velx, vely, nodepressure, startvelx, startvely

6.8.2 Fluid Navier-Stokes Equations Axisymmetric

Elements: Plane continuum (tri6, quad8)

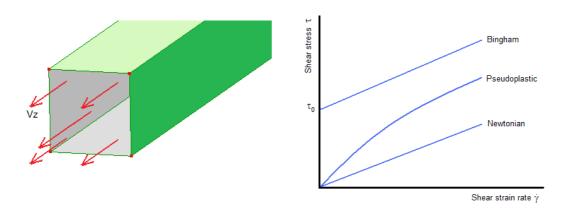
Loads and constraints: velx, vely, nodepressure, startvelx, startvely

6.9 Fluid Non-Newtonian Conduit Cross-Section

Elements: Plane continuum (tri3, tri6, quad4, quad8)

Loads and constraints: Pressure Gradient Z, velz

In this analysis type the 2D model represent the cross-section of a uniaxial pressure driven flow through an arbitrarily shaped conduit. The fluid can be an incompressible, non-Newtonian fluid represented by the Herschel-Bulkley model. Examples of such fluids are crude oils, slurries and suspensions.



LISA calculates an effective viscosity $\tau/\dot{\gamma}$ according to the following formula

$$\tau = K \dot{\gamma}^n + \tau_0$$

K: consistency index

n: flow behaviour index

то: critical shear stress

For a Bingham fluid, n=1. For a pseudoplastic fluid, τ_0 =0. For a Newtonian fluid n=1, τ_0 =0, and K=dynamic viscosity.

You should apply a Pressure Gradient Z load to all elements participating in the pressure driven flow. Boundary conditions can be applied at nodes to give a no-slip condition (velz=0), zero shear (default) or fixed velocity in Z (velz \neq 0).

6.10 DC Current Flow

Elements: Solid continuum (tet4, tet10, pyr5, pyr13, wedge6, wedge15, hex8, hex20), shell (tri3, tri6, quad4, quad8, quad9), resistor (line2)

Loads and constraints: Voltage, Current, Robin Boundary Condition, Coupled DOF

This analysis type finds the electric potential (voltage relative to an arbitrary zero) distribution throughout a structure. This electric potential which is the single DOF at each node, is then used to obtain current density, resistive power loss (ohmic heating) and current in resistor elements.

6.11 Electrostatic

Electrostatic analysis models static electric fields in insulating dielectric material.

You can specify the **Permittivity of free space** (8.854187818×10⁻¹² F/m) for the model and relative permittivities on materials.

Each node's DOF is electric potential (voltage relative to an arbitrary zero) so electric potential should be constrained at at least one node to ensure a unique solution. The solver then uses the electric potential field value to obtain the electric field and flux density.

6.11.1 Electrostatic 2D

Elements: Plane continuum (tri3, quad4)

Loads and constraints: Voltage, Charge, Robin Boundary Condition, Coupled DOF

6.11.2 Electrostatic 3D

Elements: Solid continuum (tet4, tet10, pyr5, pyr13, wedge6, wedge15, hex8, hex20)

Loads and constraints: Voltage, Charge, Robin Boundary Condition, Coupled DOF

6.12 Magnetostatic 2D

Elements: Plane continuum (tri3, quad4)

Loads and constraints: Current, Magnetic Vector Potential, Robin Boundary Condition, Coupled DOF

Magnetostatic analysis models a static magnetic field caused by conductors carrying current perpendicular to the plane of the model.

You can specify the **Permeability of free space** (1.256637061×10⁻⁶ H/m) for the model and relative permeabilities on materials.

Each node has a single DOF which is the Z component of the magnetic vector potential. From this field value the solver generates a description of the magnetic field as B and H vector fields.

6.13 Acoustic Cavity Modes

This analysis type can find vibration modes of fluid in an enclosed cavity such as sound resonance in a room or vehicle cabin. It cannot model openings in the walls of the cavity such as windows or doors. If you need to model an opening in an object, you need to embed the object in a larger 'room' which itself is fully closed. However, you will then need to distinguish the acoustic behavior of the object from that of the enclosing room.

The modes are solutions to the Helmholtz equation

$$\nabla^2 \mathbf{p} + (\omega/\mathbf{c})^2 \mathbf{p} = 0$$

where p is the pressure relative to ambient, ω is the angular frequency of the mode, and c the speed of sound in the medium.

Continuum elements represent the medium inside the cavity. Boundary faces without any constraints behave like hard surfaces with the following Neumann boundary condition

$$\nabla \mathbf{p} \cdot \mathbf{n} = \mathbf{0}$$

where \underline{n} is the surface normal vector. This means some of the pressure anti-nodes will occur at the boundaries.

The mode shapes (pressure) shown in the solution are the instantaneous pressure of the standing waves which will oscillate sinusoidally with time. Their amplitudes are arbitrary. The mode frequencies shown in the solution are the angular frequencies ω .

6.13.1 Acoustic Cavity Modes 2D

Elements: Plane continuum (tri3, tri6, quad4, quad8)

Loads and constraints: nodepressure

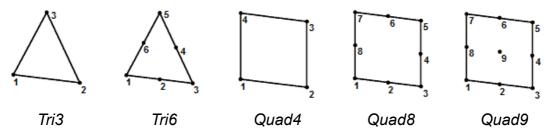
6.13.2 Acoustic Cavity Modes 3D

Elements: Solid continuum (tet4, wedge6, hex8)

Loads and constraints: nodepressure

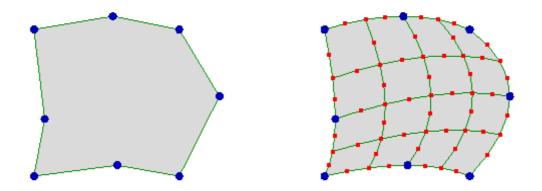
Elements

7.1 Plane Continuum Elements



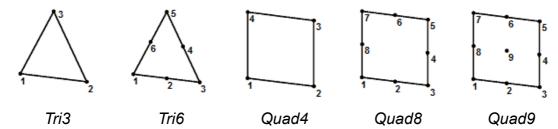
Plane elements can be used for various 2D analysis types to represent structures such as flat plates or prismatic rods. Their nodes should lie in the XY plane.

The quadratic elements (those with midside nodes) can have parabolically curved sides although they are displayed as being straight. You can see the curved shape by refining the element as shown below.

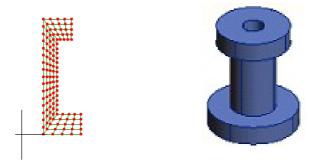


Quadratic elements typically perform better than the linear elements because the DOF field value can vary quadratically along their edges whereas the linear elements only allow a linear variation. In mechanical analysis types the linear elements, especially tri3 (constant strain triangle), have a further limitation of being too stiff in bending. To model bending accurately with linear elements you must refine the mesh so that each individual element experiences mostly tension or compression and less bending.

7.2 Axisymmetric Continuum Elements

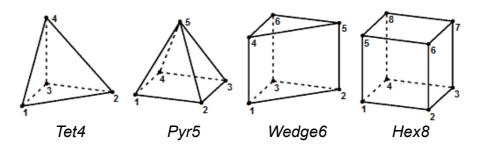


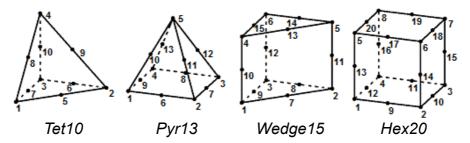
Although these appear to be the same as plane continuum elements, each axisymmetric element actually represents an entire circular solid as shown below. The axis of symmetry is the Y-axis and elements must be located in the X-Y plane with all X-coordinates non-negative. Axisymmetric elements can only be used in the axisymmetric analysis types.



In mechanical analysis types, each node has 2 DOFs: displacement in X(radial) and displacement in Y(axial). Any nodes located at X=0 must be restrained to not be displaced in the X direction because it is physically unreasonable that the material should overlap itself or for a hole to appear. Also, rigid body motion can only occur by translation along the Y-axis, so only translational motion in the Y direction needs to be constrained to prevent rigid body motion.

7.3 Solid Continuum Elements

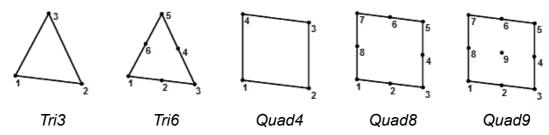




Solid elements are the most general and, in principle, can be used to model any shaped structure. However some geometries such as thin beams or plates can require a such a large number of solid elements that the solver runs out of memory or takes too much time. In these cases you can further idealize the model by using shells, beams, fins, resistors, etc. instead of solid elements.

In mechanical analysis types, hex20 typically performs much better than all the other solid elements. This means you attain the same accuracy with fewer elements.

7.4 Shell



Shells are 3D elements that can model stress, heat flow or electric current in the plane of the element but not through the thickness. They are useful for thin parts where solid elements are too computationally expensive or in place of 2D elements where those are not available. Typical structures modeled with shell elements include sheet metal brackets and cabinets, thin metal platforms, pressure vessels, and body parts of motor vehicles.

In the mechanical analysis types, the elements use Mindlin thick plate theory which models out-of-plane bending and shear stiffness. They also incorporate plane stress membrane stiffness for in-plane deformation in the same way as the 2D membrane elements. Each node has 6 DOFs – displacement in X, Y and Z and rotation about X, Y and Z. However there is no drilling DOF which means each node is free to rotate about the shell's normal and is only resisted by an arbitrary small stiffness to ensure numerical stability. The tri3 shape is not available for static analysis and only quad8 is available in modal vibration.

The rotational DOFs of shells mean that you can join two shell elements together at a common edge and they will transmit bending moments between each other. This is distinct from solid elements which cannot transmit bending moments when they're only connected by an edge. If the straight edge of a shell is joined to the edge of a solid element, then it will form a hinge joint. To make a stiff joint, overlap the two elements.

In modal vibration, shells use consistent mass matrices with no rotational inertia at the nodes. This simplification typically doesn't cause problems because the effect of nodal rotational inertia vanishes with mesh refinement.

Each element has a local right-handed coordinate system U,V,W which is used for orienting orthotropic and laminate materials and for displaying some stress results. The W axis is normal to the element's surface. By default U is parallel to the edge from nodes 1 to 2, or 1 to 3 for linear or quadratic elements respectively. You can define the direction of the U axis by specifying a vector in global X,Y,Z coordinates. The direction of the U axis is the projection of this vector onto the plane normal to W. The V axis is mutually perpendicular to U and W.

Shell elements can be curved out of their plane but should be approximately flat because they are internally projected onto a 2D plane by the solver. Because of this, warped or doubly curved elements in mechanical analysis types can have slow convergence or may fail to converge at all with mesh refinement as shown in the sample TwistedBeam.liml.

The best accuracy and fastest convergence is typically obtained with the quad8 or quad9 shells. LISA uses various integration schemes for the different physical phenomena in each element shape as shown in the following table.

Number of integration points	tri3	tri6	quad4	quad8	quad9
membrane	N/A	7	4	9	9
bending	N/A	7	4	9	9
shear	N/A	7	1	4	9
thermal	1	7	4	9	9
DC current	1	7	4	9	9

Stress results for shells in static analysis are obtained from bending moments and membrane forces. Out-of-plane shear forces are disregarded. Stresses are not reported for laminate materials or modal vibration.

LISA reports **von Mises Stress** and the two in-plane **Principal Stress**es at three locations: the upper surface of the element, the midplane and the bottom surface of the element. The upper surface is the surface with a more positive W coordinate. The display shows all three results simultaneously when **Show thickness** is turned on, and shows only the upper and bottom stresses otherwise.

Stress UU, **Stress VV** and **Stress UV** are the membrane (midplane) stress components in the local element coordinate system. Because the shell has thickness, in bending, its stress will be different away from the midplane.

Moment U, Moment V and **Moment UV** are moments per unit length for out-of-plane bending and twisting. They are with respect to the local coordinate system of the element. Moment U is bending about the local V axis, and Moment V about the local U axis. Moment UV is the twisting (torsion) moment per unit length.

Shear UW and **Shear VW** are out-of-plane shear force per unit length. Divide by thickness to obtain the average shear stress components. Actual shear stress varies through the thickness.

7.5 Beam

LISA's beam elements use Euler beam theory which means they can model bending of slender, uniform, isotropic beams. They also have longitudinal and torsional stiffness allowing them to act as



Line2

columns or shafts. Each node has both displacement and rotational DOFs so they can transmit bending and twisting moments between elements.

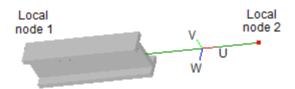
You can apply loads and constraints to the end faces or the side face.

An a arbitrary cross sectional shape (**General section**) can be defined by its geometric properties, or various predefined shapes can be used depending on the analysis type:

static 3D modal vibration 3D modal response 3D	I rectangular bar rectangular tube circular bar circular tube general section
static 2D	C T I rectangular bar rectangular tube circular bar circular tube general section
modal vibration 2D modal response 2D buckling 2D	general section

The orientation of the beam cannot be fully defined by the locations of the nodes alone so there are other options to control how the cross section is rotated about the beam's longitudinal axis. These are available under **Element properties**.

In 3D, the element's local coordinate system, U, V, W defines the orientation of the cross-section.



The U axis is parallel to the element's length, the V axis is perpendicular to U and the W axis is mutually perpendicular to both U and V according to W=U×V. These constraints leave the V axis free to rotate about the element's longitudinal axis. There are two options for defining the direction of the V axis:

- **Default**. The V axis is perpendicular to the global Z axis and parallel to the XY plane. If the element is nearly parallel to the Z axis (gradient < 0.01%) then the V axis is made parallel to the Y axis too.
- **Direction of element V axis**. The V axis can be defined by a vector in the global X, Y, Z coordinate system. The specified vector might not meet the requirement of being perpendicular to U, so the V axis is the projection of this vector onto a plane perpendicular to U. This allows almost any vector to be used a long as it is not zero (0, 0, 0) and not be parallel to U. The magnitude of the vector is not used by LISA.

After defining the vector you can also apply a further rotation of V about U by a specified angle (**Rotate by angle**). This feature is useful if you know the angle in which you want to orient the beam but don't want to manually convert it to vector form. It can also be helpful if you want to specify a common direction of W for many elements in different orientations. You can set the vector to the direction of W then rotate it by -90°.

In 2D, the U, V, W element coordinate system is fully defined by the locations of the element's nodes, with W parallel to the global Z axis and in the same direction. However the orientation of the cross-section can be flipped so that it is still symmetric about the XY plane. Choosing the **2nd orientation** option will rotate I, rectangular bar and rectangular tube sections by 90° and C and T sections by 180°.

Beam stresses and forces are reported in static analysis only. Tensile stresses are the stresses at each of 4 predefined points in the cross-section and one user-defined **Stress recovery point in principal coordinates**. These stress values are calculated only from the normal force and bending moments. They do not incorporate shear stress caused by torsion or shear forces.

The results in static analysis show the forces and stresses at each end of each element. However the values at nodes are the averages of the elements connected to those nodes so these will often be misleading. You can display non-averaged values in the contour plot by selecting **Element Values** from under the relevant force or stress branches in the outline tree. You can also click on a node in the graphics area to show the values at all its adjacent elements.

7.6 Truss

A truss element is a beam hinged at both ends so that it can only resist axial compressive or tensile forces and has no bending or torsional stiffness. Each node has translational degrees of freedom in the the X. Y and, if 3D, Z directions.



Line2

Truss elements can be used to model truss structures where no bending occurs in individual members, as well as to transmit forces between objects and create hinge joints between beam or shell elements.

To convert a beam element into a truss element, select the desired elements, right click on one of them, click **Element properties** and check **Truss**.

Only static 3D models can use all the uniform section shapes (C, T, L, I, rectangular bar, rectangular tube, circular bar, circular tube and general section) for trusses. Static 2D disallows L section, and in other analysis types only the general section can be used. No orientation needs to be specified like for beam elements.

The results in static and dynamic response show the axial force and stress at each end of each element. However the values at nodes are the averages of the elements connected to those nodes so these will often be misleading. You can display non-averaged values in the contour plot by selecting **Element Values** from under the **Tensile Force** or **Tensile Stress at User Defined Point** branches in the outline tree. You can also click on a node in the graphics area to show the values at all its adjacent elements.

7.7 Axial Spring



Line2

The axial spring element has stiffness only in the direction of its length and is hinged at its endpoints. It can be used anywhere that a truss element can. Each node has 2 or 3 translational degrees of freedom along the X, Y and Z axes depending on the number of dimensions (2D or 3D).

You can define an axial by applying the **Spring** mechanical material type to a line2 element. You can also specify the spring constant and free length.

The **Spring constant** k is the stiffness in Hooke's law

$$F = -k u$$

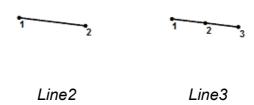
where F is the extending force exerted by the spring and u is the increase in length from the free length.

Free length is useful in static and buckling analysis only. It allows the spring to be preloaded to the element's modeled length and it will produce its own restoring force when solved. If you don't specify a value for free length then it defaults to the element's modeled length.

A spring element behaves identically to a truss element with zero density. The equivalent truss element satisfies the equation

cross-sectional area x Young's modulus = spring constant x length

7.8 Fin



The rate of heat removed by convection from a surface is increased by increasing the surface area for heat transfer using extended surfaces called fins. A simple example is a metal spoon placed in a glass of hot water, heat is conducted through the spoon to cause the handle to become warmer than the surrounding air. Heat is then transferred from the spoon handle to the air by convection. Similarly, industrial applications use fins in car radiators, double pipe heat exchangers, electronic equipment and compressors.

A fin element models heat conduction along its length but not across its width. It can also have convection and radiation heat transfer applied to its side face and/or end faces.

7.9 Resistor



Line2

A resistor element has a linear change in potential over its length according to Ohm's law V=IR. It's resistance can be defined by either using the single extensive property resistance, or by its material's conductivity together with the geometry of a beam. Any of the uniform section shapes (C, T, L, I, rectangular bar, rectangular tube, circular bar, circular tube, general section) can be used.

Resistors can be useful for modeling linear electric circuits as well as for measuring current values in 3D continuum or shell models. To find the current flowing through a complex object, you can place a resistor element with near-zero resistance in series with the object. The solution will then show the current flowing in the resistor.

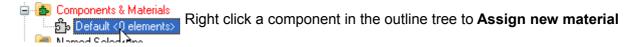
Materials

Elements are designed to mathematically represent various types of materials for both their physical properties and their geometric shapes.

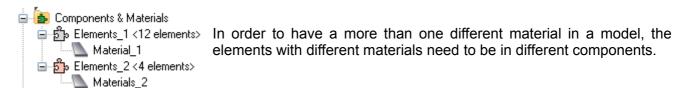
8.1 Materials database

LISA does not provide a materials database. If you find yourself using the same materials repeatedly, create an empty LISA file with only the materials defined in it, then when you need a material, open it using **Load into model** from the **File** menu. This will import those materials into the currently open model.

8.2 Defining a new material



8.3 Mixed materials



The 3D automesher can't make parts with defined boundaries between different material types. To get a perfect boundary between different materials, mesh it manually or use the automesher for the more complex part then manually build the simpler part onto it.

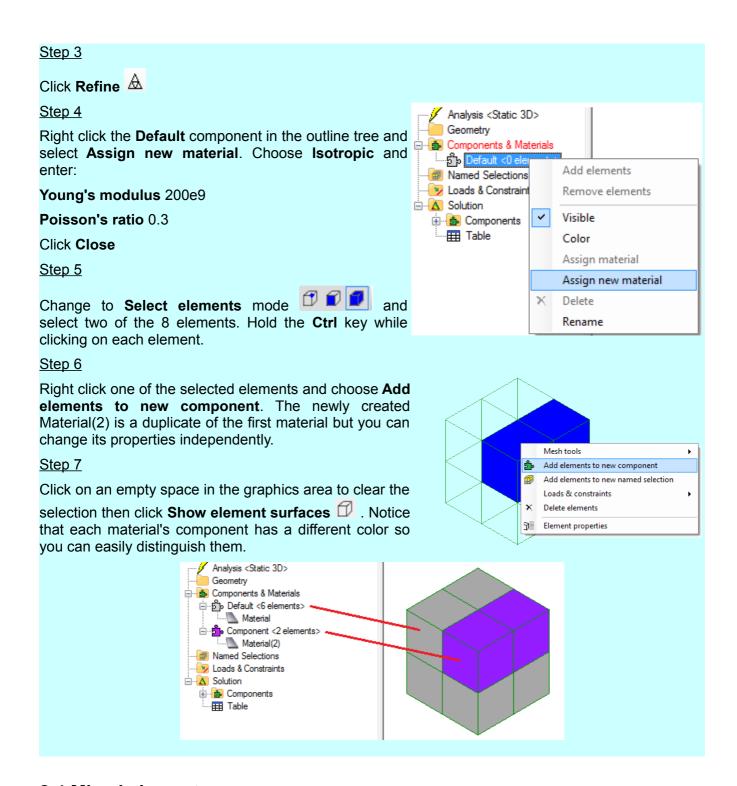
8.3.1 Mixed material tutorial

Step 1

Open a new instance of LISA.

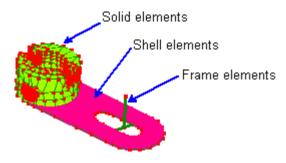
Step 2

Click Quick cube



8.4 Mixed elements

Element types can be mixed in the same model, but each should have its own material definition because their geometrical properties are not the same.



8.5 Orthotropic & anisotropic materials

Orthotropic materials have mechanical properties that differ along directions which are perpendicular with each other. In LISA, orthotropic materials can be specified for 3D solid, 2D membrane and shell elements. For solid elements, the properties will differ along the global X, Y, Z-axis directions. For 2D membrane elements, the properties will differ along the global X & Y-axis directions. For shells, the properties will differ along their local U, V co-ordinate axes rather than the global X, Y, Z-axes. The local axes of shells can be displayed using this tool-button

Anisotropic materials have mechanical properties that differ along arbitrary directions which are not perpendicular with each other.

In LISA, Young's modulus can be defined separately for each direction of orthotropic materials and for anisotropic materials the coefficients of the elasticity matrix are specified.

8.6 Temperature dependent properties

You can specify temperature dependent thermal conductivities and specific heat values. The solver linearly interpolates between the specified data points. If a temperature is outside of the range, the solver uses the nearest data point rather than attempting to extrapolate.

Loads and Constraints

9.1 Fixed Support

Analysis types: Static, Modal Vibration, Modal Response, Dynamic Response, Buckling

A fixed support constrains all the face's nodes against displacement in any direction. If any nodes have rotational degrees of freedom then those are also constrained against rotation.

A fixed support can only be applied to a named selection containing faces.

9.2 Displacement

Analysis types: Static, Modal Vibration, Modal Response, Dynamic Response, Buckling

A displacement constraint enforces the specified displacement on every node in the named selection it is applied to. The displacement is only constrained in the specified direction and the nodes are free to move in perpendicular directions.

A displacement can be applied to a named selection containing nodes, faces or elements.

To constrain displacement in an arbitrary direction other than of one of the global X, Y or Z axes, you can rotate the nodes' coordinate systems by applying transformrx, transformry and/or transformrz to the nodes. This is useful for sliding supports on inclined surfaces.

In modal vibration, modal response, dynamic response and buckling the displacement must be zero.

9.3 Flexible Joint

Analysis types: Static 3D

A flexible joint releases the rotational stiffness of the end of a beam element allowing it to rotate freely even when it's connected to another element or has constrained rotation.

A flexible joint must be applied to named selections containing only end faces of beam elements.

The joint can allow rotation about any combination of the three local axes (U,V,W) of the beam element. The meaning of some combinations are:

- U The element can rotate about its own axis like being connected to a roller bearing.
- V or W A pin joint which allows the element to pivot about one axis.

- V and W A universal joint which transmits torque but not bending moments.
- U,V and W A ball joint which allows the element to rotate in any direction.

9.4 Force

Analysis types: Static, Modal Vibration 3D Solid and Truss, Modal Response, Dynamic Response, Buckling

A force applied to faces is distributed over the faces as a uniform traction with the same direction at every point and with a total magnitude equal to the magnitude specified. A force applied to nodes is divided equally between the nodes.

A force can be applied to a named selection containing nodes or faces. It can be constant or time dependent.

The force vector must be specified in global X, Y, Z coordinates.

9.5 Pressure

Analysis types: Static, Modal Vibration 3D Solid and Truss, Modal Response, Dynamic Response, Buckling

Pressure applies a force proportional to the area of the face. The direction of the force can be either normal to the face or specified in global X, Y, Z coordinates. For a normal pressure, a positive value directs the force in the opposite direction to the face normal, which is inwards for volume elements.

A pressure can only be applied to a named selection containing faces. It can be constant or time dependent. It can be used with most types of element used in the mechanical analysis types: plane continuum, solid continuum, axisymmetric continuum, shell, beam and truss but not axial spring elements because they have no surface area.

9.6 Line Pressure

Analysis types: Static, Modal Vibration 3D Solid and Truss, Modal Response, Dynamic Response, Buckling

Line pressure applies a uniform force per unit length to each face in the selection. The direction of the force can be specified in either global X, Y, Z coordinates or element U, V, W coordinates when applied to the edge faces of beam or truss elements.

A line pressure can only be applied to a named selection containing faces that are locally 1-dimensional. This includes the edges of plane and line elements such as shells and beams. It can be constant or time dependent.

9.7 Moment

Analysis types: Static 2D, Static 3D, Modal Response 2D Beam, Modal Response 3D Beam, Buckling 2D Beam

Moment applies a moment to the specified node. The direction of the moment vector is specified in global X, Y, Z coordinates. The moment is directed around this vector according to the right-hand grip rule.

A moment can only be applied to a named selection containing a single node which has rotational degrees of freedom. That is, the node should be part of a beam or shell element. It can be constant or time dependent.

9.8 Gravity

Analysis types: Static, Modal Vibration 3D Solid and Truss, Dynamic Response, Buckling

Gravity gives a distributed force to all massive parts of a model. This includes elements whose material has density and nodes with point mass loads applied to them. Specify a vector which is the force per unit mass. For Earth gravity in SI units you can use Y=-9.81.

9.9 Centrifugal Force

Analysis types: Static, Modal Vibration 3D Solid and Truss, Buckling

Centrifugal Force simulates rotation of the entire model and its global coordinate system. This gives every massive part (node or element) an outward force whose magnitude is

$$F = m \omega^2 r$$

where m is the part's mass, ω is the angular velocity and r is the distance from the axis of rotation. The axis of rotation must be one of X, Y or Z. To convert rotational speed in RPM to radians/s for angular velocity, multiply by $2\pi/60$.

9.10 Tension Per Length

Analysis types: Modal Vibration 2D Transverse Vibration of Membrane

This load applies a uniform 2D isotropic stress over all the elements in the model.

9.11 Temperature

Analysis types: Static, Modal Vibration 3D Solid and Truss, Buckling, Thermal

In a thermal analysis a temperature load constrains the temperature to the specified value at the items in the named selection. Heat is allowed to flow into or out of the model at these locations to maintain the specified temperature.

In a static or buckling analysis the temperature is used for thermal stress where a thermal stress load must also be applied.

Temperature can be applied to a named selection containing nodes, faces or elements.

The temperature can be constrained within a specified time interval in a thermal transient analysis. Within this interval, a constant or time-dependent temperature can be specified. In steady state analysis, temperature must be specified as a single constant without any time interval.

9.12 Thermal Stress

Analysis types: Static, Modal Vibration 3D Solid and Truss, Buckling

When present, thermal stress enables thermal loading. A single reference temperature must be specified as well as temperatures on parts of the model and thermal expansion coefficients in the materials.

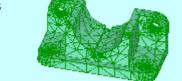
The difference between each element's average specified temperature and the reference temperature is used to determine the thermal expansion/contraction loads. Any nodes that don't have a specified temperature are assumed to be at the reference temperature.

Only one thermal stress can be applied in a model.

9.12.1 Thermal stress tutorial

Step 1

Open **ThermalStressTutorial.liml** from the tutorials folder where LISA has been installed.



Analysis < Thermal Steady State>

We will perform a thermal analysis first.

Step 2



Right click Surface10 and select New loads & constraints → New

temperature

Named selection Surface 10

Constant 80

Repeat for Surface 14

Step 3



Right click Surface20 and select New loads & constraints → New

convection

Named selection Surface 20

Ambient temperature 22 Heat transfer coefficient 400

Repeat for Surface 21 and Surface 22

Step 4 Solve Step 5 Right click Analysis and select Edit Analysis Type tab Static 3D 🕖 Analysis <Static 3D> Step 6 Loads & Constraints Right click Loads & constraints and select Transfer temperatures from solution Step 7 🎒 Loads & Constraints Right click Loads & constraints and select New thermal stress Reference temperature The reference temperature is the initial temperature of the nodes that are now at the temperatures which were transferred from the thermal analysis solution. Step 8 🚊 நீ Meshed_Geometry <3505 elements> Right click Material and select Edit **Mechanical** tab Isotropic Young's modulus 200E09 **Density** 7800 Thermal expansion coefficient 11E-06 Step 9 Right click Surface2 and select New loads & constraints → New fixed 🖃 🝘 Named Selections Surface2 < 242 faces> support

Step 10

Solve

9.13 Pressure Gradient Z

Analysis types: Fluid Non-Newtonian Conduit Cross-Section

This load specifies the Z component of the pressure gradient through the elements in a named selection. This pressure gradient can drive the fluid's flow in the Z direction.

9.14 Heat Flow Rate

Analysis types: Thermal

Heat is added to the model at the specified rate. It is distributed uniformly across the volume or surfaces it is applied to. If it is applied to nodes then the specified heat flow rate is divided equally between each node.

Heat Flow Rate can be applied to a named selection containing nodes, faces or elements.

A time-dependent Heat Flow Rate can be specified as a table of time and value pairs.

9.15 Internal Heat Generation

Analysis types: Thermal

Heat is added to the model at a uniform rate over the volume it applies to. The value specifies the rate at which heat is added to the model per unit volume.

Internal Heat Generation can be applied to a named selection containing elements.

A time-dependent Internal Heat Generation can be specified as a table of time and value pairs.

9.16 Flow Rate

Analysis types: Fluid Potential Flow

Fluid enters the model at the specified volumetric flow rate uniformly across the volume or surface it is applied to. If it is applied to nodes then the specified flow rate is divided equally between each node.

Flow Rate can be applied to a named selection containing nodes, faces or elements.

9.17 Voltage

Analysis types: DC Current Flow, Electrostatic

Voltage applies a uniform voltage over every item in the named selection. All applied voltages in a model are relative to a common ground.

9.18 Charge

Analysis types: Electrostatic

Charge defines an electric charge uniformly distributed across the volume or surface it is applied to. If it is applied to nodes then the specified charge is divided equally between each node.

Charge can be applied to a named selection containing nodes, faces or elements.

9.19 Current

Analysis types: DC Current Flow, Magnetostatic

Current defines an electric current flowing into the model and uniformly distributed across the surface it is applied to. If it is applied to nodes then the specified current is divided equally between each node.

Current can be applied to a named selection containing faces or nodes.

A positive value on the face of an element represents current flowing into the element. In 2D magnetostatic analysis the current only flows parallel to the Z axis. Here a positive value on a node represents current flowing in the positive Z direction.

A winding of many turns in magnetostatic analysis can be modelled by a single current who's value is the sum of the currents in all the turns.

9.20 Magnetic Vector Potential

Analysis types: Magnetostatic

A magnetic vector potential boundary condition constrains the Z-component of the vector potential to the specified value over the faces or nodes that it is applied to. This is a Dirichlet boundary which has the effect of preventing flux lines from crossing the boundary. It can be used on the outside boundary to contain the flux within the domain.

Magnetic vector potential can only be applied to named selections containing faces or nodes.

9.21 Convection

Analysis types: Thermal

Convection allows heat flow into or out of a face according to a specified heat transfer coefficient and ambient temperature.

Convection can only be applied to a named selection containing faces.

9.22 Radiation

Analysis types: Thermal

Radiation allows heat flow into or out of a face according to a specified emissivity and ambient temperature. The Stefan-Boltzmann constant must also be specified in the model.

If radiation is used then all temperatures in the model must be specified in absolute units such as kelvin or degrees Rankine.

Radiation can only be applied to a named selection containing faces.

9.23 Robin Boundary Condition

Analysis types: DC Current Flow, Electrostatic, Magnetostatic

The Robin Boundary Condition imposes the following equation on a face

 $k \frac{\partial u}{\partial n} + c_0 u + c_1 = 0$

where

- *u* is the degree of freedom, either electric potential or magnetic potential depending on the analysis type
- *k* is either the electrical conductivity, absolute permittivity or absolute permeability of the material
- $\partial u/\partial n$ is the normal derivative of u at the face
- c_0 and c_1 are user specified parameters. If $c_0 = 0$ this is a Neumann boundary condition, constraining the field value's gradient normal to the face.

A Robin Boundary Condition can only be applied to a named selection containing faces.

9.24 Cyclic Symmetry

Analysis types: Static 3D, Modal Vibration 3D Solid and Truss, Thermal Steady State

If geometry and loading are regularly repeated about an axis of rotation, then cyclic symmetry (rotational periodicity) can be used to reduce the model to only one segment, allowing a smaller mesh and improved solver performance.

Two named selections must be specified: one contains the nodes on one of the cut surfaces and the other contains nodes on the other surface. These two sets of nodes must have the same layout so that each node on one surface coincides with one node on the other surface when the segment is rotated.

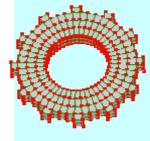
If displacement constraints are applied to nodes on the cut surfaces, their directions will be rotated from X, Y, Z to radial, circumferential and tangential.

In thermal analysis cyclic symmetry is equivalent to applying coupled DOF between the corresponding pairs of nodes on the cut surfaces.

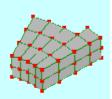
In static analysis cyclic symmetry is equivalent to applying transformed coordinates to the nodes of the cut surfaces and coupling their degrees of freedom.

In modal vibration analysis cyclic symmetry applies transformed coordinates and couples the degrees of freedom using special complex constraints.[2] This method can find modes which are not cyclically symmetric. The number of modes specified for the solution is not the total number of modes, but the number of modes having the same number of nodal diameters. For example if 5 modes are specified in a model with 7 segments, the solver will find the lowest 5 modes with each of 0, 1, 2 and 3 modal diameters, leading to a total of 20 modes.

9.24.1 Cyclic symmetry tutorial

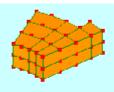


Instead of modeling the entire wheel using solid elements, only one segment will be modeled using cyclic symmetry.



Step 1

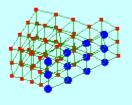
Open **CyclicSymmetryTutorial.liml** from the tutorials folder where LISA has been installed.



Step 2

Activate Select nodes

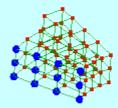
Hold the **Ctrl** key down and select these four nodes with the mouse.



Right click on the selected nodes and select Add nodes to new named selection.

Click a blank part of the graphics area to deselect the nodes

Hold the **Ctrl** key down and select these nodes with the mouse.



Right click on the selected nodes and select Add nodes to new named selection.

Step 3

Right click Loads & Constraints and select New cyclic symmetry.

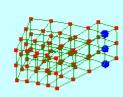


Master named selection Unnamed Slave named selection Unnamed(2)

Axis of symmetry Y Number of segments 12

Step 4

Select the 3 nodes shown here. Right click on one of the selected nodes and select **Loads & constraints** \rightarrow **New displacement**.



Axis X Value 0

The nodes are now constrained circumferentially and can only move radially and axially.

9.25 Stress Stiffening

Analysis types: Modal Vibration 3D Solid and Truss

The stress state of a structure can influence its stiffness and vibration modes. LISA can account for this by first performing a static analysis to determine the stress state then performing a modal vibration analysis using a modified stiffness matrix.

When Stress Stiffening is applied a static analysis will be run automatically before the modal vibration. Loads should also be applied to induce stress. All the load types available for the corresponding static analysis elements can also be used for stress stiffening except for non-zero displacements.

Tensile stress tends to stiffen a structure and increase the natural frequencies. Compressive stress tends to reduce the frequencies. If compressive stress is too high it may exceed the buckling load of a structure. In these cases LISA may produce non-physical modes with frequencies of "NaN".

9.26 Loads and Constraints on Nodes

Some loads and constraints can be applied to individual nodes instead of named selections. These can allow direct control of the value at each node but they are not interpolated during mesh refinement and are removed by some mesh tools.

To apply these loads or constraints, right click on a node, select **Loads & constraints** then **On selected nodes**. To change their values or delete them select **Edit** from the **On selected nodes** menu. Alternatively, you can select nodes first then right click **Loads & Constraints** in the outline tree then select **On selected nodes**.

9.26.1 rotx, roty, rotz

Analysis types: Static 2D, Static 3D, Modal Response 2D Beam, Modal Response 3D Beam, Modal Vibration 2D Beam, Modal Vibration 3D Shell and Beam, Buckling 2D Beam

Each of these constraints fixes the rotation angle of it's node about the relevant axis (X, Y or Z). The angle is measured in radians. You can only use them on nodes having the corresponding rotational DOFs. This includes nodes of beam and shell elements but not solid or plane continuum elements.

In some analysis types you can also constrain rotation about another axis besides one of X, Y or Z. Do this by rotating the node's coordinate system using transformrx, transformry and/or transformrz.

9.26.2 velx, vely, velz

Analysis types: Fluid Navier-Stokes Equations, Fluid Non-Newtonian Conduit Cross-Section

Each of these constraints fixes one component of a fluid's velocity.

In the Fluid Navier-Stokes Equations analysis type, you can model a no-slip boundary condition by applying velx=0 and vely=0 on all the nodes of the boundary. You can model a symmetry plane by setting only one component to zero to prevent fluid flow through the plane of symmetry. You can model a known flow rate by setting both velx and vely to the two components of the fluid's velocity.

In the Fluid Non-Newtonian Conduit Cross-Section analysis type, you can only use velz. This constrains the velocity in the out-of-plane direction. The in-plane (X and Y) velocity components are always zero.

9.26.3 nodepressure

Analysis types: Fluid Navier-Stokes Equations, Acoustic Cavity Modes

In Fluid Navier-Stokes Equations, nodepressure constrains the fluid's pressure at the specified node. Only the corner nodes of elements have pressure DOFs, so nodepressure applied to midside nodes will be ignored by the solver.

In the Acoustic Cavity Modes analysis type, you can use nodepressure=0 to enforce a pressure "node". Node here means a location where the pressure remains zero throughout the wave's cycle. Any non-zero value of nodepressure will be treated as zero.

9.26.4 startvelx, startvely

Analysis types: Fluid Navier-Stokes Equations

These set initial values of velocity's X and Y components for the iterative solver to begin with. The solution will converge faster if it starts near the solution. They are not typically needed unless you want to optimize the speed or there is an instability which causes the solver to fail to converge otherwise.

9.26.5 velocitypotential

Analysis types: Fluid Potential Flow

Velocitypotential constrains the velocity potential on a node. You can create an inlet or outlet by setting zero velocity potential on all the nodes of a boundary. This causes the flow direction to be normal to the boundary.

9.26.6 nodetemperature

Analysis types: Static, Modal Vibration 3D Solid and Truss, Buckling, Thermal

Nodetemperature fixes the temperature of a node and is similar to the Temperature load which can be applied to named selections. Nodetemperature can be more convenient for a temperature field whose value is different on every node because you can create a large number of them without making a separate named selection and separate outline tree item for every node.

A common use for nodetemperature is thermal stress analysis where the values are generated by the solver in a thermal analysis then used as input for a static analysis.

9.26.7 transformrx, transformry, transformrz

Analysis types: Static, Modal Vibration 3D Solid and Truss, Buckling 3D

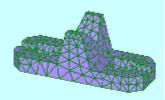
If you need to constrain displacement or rotation in a direction which is not orthogonal to the X,Y,Z global coordinates then you can rotate the coordinate system of each node. Displacement constraints, rotation constraints (rotx, roty, rotz) and coupled DOF applied to these rotated nodes will be oriented in the new direction.

Transformrx rotates the node's coordinate system about the X axis by the specified number of degrees. Similarly, transformry and transformrz rotate it about the Y and Z axes respectively. You can define an arbitrary orientation by specifying two or all of transformrx, transformry and transformrz on the same node. When more than one rotation is applied to the same node, they are applied in this order: Rotation about Z then rotation about Y then rotation about X.

Inclined supports tutorial

Step 1

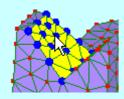
Open **InclinedTutorial.liml** from the tutorials folder where LISA has been installed.



Step 2



Activate Select nodes



Select the nodes shown here. Right click on one of the selected nodes and select Loads & constraints → On selected nodes → New transformrx Value 45

Step 3

With the nodes of the previous step still selected, right click one of the selected nodes and select **Loads & constraints** \rightarrow **New displacement**. Click **OK**



A frictionless sliding support is now enforced along the inclined surface.

9.26.8 mass

Analysis types: Static, Modal Response, Modal Vibration, Dynamic Response, Buckling

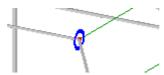
Mass is a lumped mass at a node. It can be used instead of density or to idealize a massive object without modeling it with elements. This mass affects dynamic behavior, gravity and centrifugal force. When you apply a mass to several selected nodes, the specified mass is applied to each node and not distributed between them.



9.26.9 rotationalinertiax, rotationalinertiay, rotationalinertiaz

Analysis types: Modal Response 2D Beam, Modal Response 3D Beam, Modal Vibration 2D Beam, Modal Vibration 3D Shell and Beam

These are points of additional rotational inertia about one of the X, Y or Z axes which can only be applied to the nodes of beam and shell elements. You can use them to idealize massive parts such as flywheels without modeling them using elements.



9.27 Coupled DOF

Analysis types: Static 2D, Static 3D, Thermal Steady State, DC Current Flow, Electrostatic, Magnetostatic

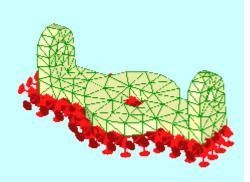
This if a form of constraint which forces a DOF (degree of freedom) of a node to have the same value as another DOF of the same or a different node. For example the X-displacement of one node can be coupled to the Y-displacement of another node so they act as if they are connected by a 90° bell crank. In thermal analysis, the temperatures of many nodes can be coupled together to form a perfectly conducting connection.

Each slave DOF can have at most one master, but a master can have any number of slaves. A slave cannot also be a master. Constraints can be applied to either the master or slave DOF of a pair, but not both. Loads can be applied to master, slave or both DOFs of a pair. If applied to both, the two loads are summed.

9.27.1 Coupled DOF tutorial

Step 1

Open **CoupledTutorial.liml** from the tutorials folder where LISA has been installed.



Step 2

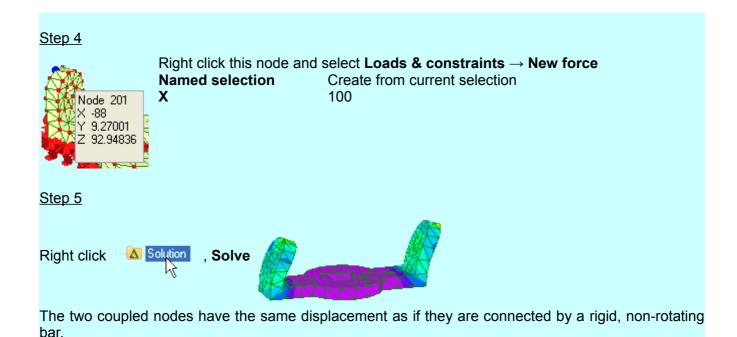
Activate Select nodes

Step 3

Right click Loads & Constraints Loads & Constraints and select New coupled DOF

Master node 201 Slave node 36

All matching pairs check-box selected



9.28 Load Cases

Analysis types: Static

Load cases allow a single computation to be performed for different sets of applied loads instead of having to create separate models for each type of loading. To combine the loads from several load cases you would have to create another load case with the duplicates of the loads in it.

Each load case includes all the loads specified under its branch in the outline tree as well as all loads and constraints specified outside any load case (directly under the Loads & Constraints branch in the outline tree). This allows common loads to be applied to all load cases without being duplicated.

Only the following loads can be used in load cases: force, pressure, line pressure, moment, temperature and nodetemperature. Constraints and gravity can only be common to all load cases.

To create a load case, right click **Loads & Constraints** in the outline tree then select **New load case**.

9.29 Time Dependent Loads

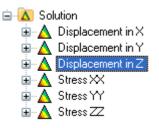
Analysis types: Modal Response, Dynamic Response, Thermal Transient

Some loads and constraints can vary as a function of time. You specify each time-dependent component as a table of time and value pairs. The solver performs a linear interpolation between data points in the table to determine the value at each time step. If a time step is outside the range of times in the table then constant extrapolation is performed so that the final value will be applied at all subsequent times and the first value will be applied at all preceding times.

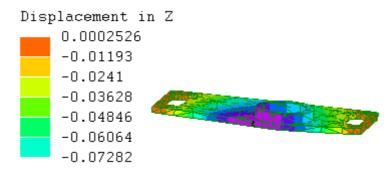
If a constant value is specified in an analysis type that allows time dependent values then the solver will use the constant value at all time steps.

Results

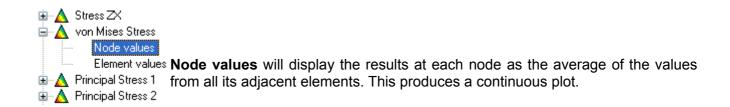
10.1 Display

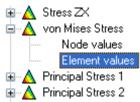


Select any item below **Solution** to display a field value as a color coded contour plot. These are only available after solving the model.



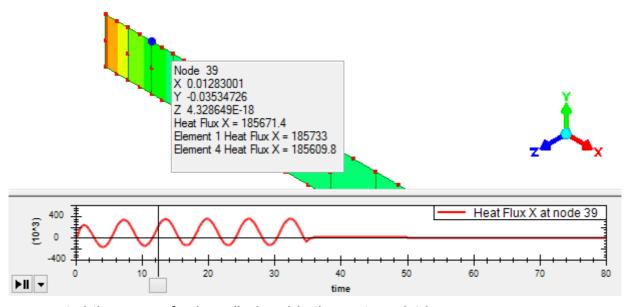
The contour plot can be configured using by selecting **Options** then **Colors** from the **Tools** menu. Here you can change the color scheme, number of colors and resolution. A higher resolution is slower to render but gives smoother boundaries between colors so it can be useful for presentation.



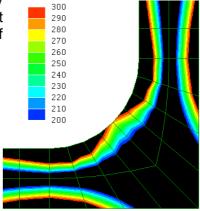


Element values will display the results without nodal averaging. Beam element results should be viewed without nodal averaging because the values of adjacent elements at joints may be very different so averaging can give meaningless results.

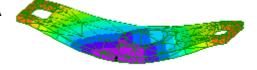
Click on a node to display both its averaged node value and the non-averaged values of all its adjacent elements. If there are time steps in the solution, the timeline will also show a graph of the node's value.



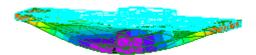
You can control the range of values displayed in the contour plot by selecting **User defined maximum and minimum** from the context menu of **Node values** or **Element values** in the outline tree. Parts of the model outside the specified range will be displayed in black.



View deformed shows exaggerated deformation. A default amplification factor is chosen automatically to give a clearly visible change. Set this to 1 to show the actual deformation.



Undeformed mesh on/off superimposes the undeformed profile on the exaggerated deformation.



View undeformed returns to an undeformed display.

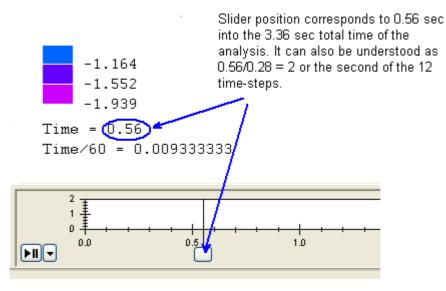
Show arrows... displays vector fields using arrows whose length and color correspond to magnitude. This option only works if the selected field value is a vector field magnitude, such as Displacement Magnitude, Velocity Magnitude or Heat Flux Magnitude. You can make the display clearer by turning off Show element surfaces and Show element edges.

works for results
For results with peline described

Animation animates the deformation. This only works for results without time steps such as static and modal vibration. For results with time steps such as dynamic response, use the timeline described below.

Time steps in transient problems are displayed on the timeline, the length of which is the total duration of the analysis. The result in the graphic display will correspond to the slider's position.

For example, consider a dynamic response analysis with **Number of time steps =** 12 and **Time step =** 0.28s. The length of the horizontal scale would be $12 \times 0.28s = 3.36s$.



To animate the display, click the play/pause button. The drop-down menu can be used to control the speed. You can use this together with **View deformed** to show movement.

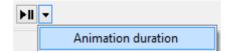


Table displays the results in a table which can be copied and pasted into a spreadsheet. The options you set here are saved with the model so you can easily generate the same table after solving again. If you enter a file name under Write to csv file after solving LISA will save the table to the

specified text file every time it solves the model. This file can be opened with a spreadsheet application or other software for further processing.

10.2 File Output

Various results can be written to files when the solver runs. Most of these options are available through the **Output Files** tab in the **Analysis** item in the outline tree. However, to write the solution data in tabulated form to a csv file, use the **Table** item under the **Solution** branch of the outline tree. This is described in the previous section.

Write solution to liml file saves the solution to the specified file. This file may not contain the complete original model, only the solution and supporting information so it can be opened again by LISA.

Write stiffness matrix to file saves the stiffness matrix to a text file. It can be stored in either a sparse or dense format. The **Dense** format contains the entire square matrix with one row on each line of the file. The **Sparse** format doesn't contain most of the zero elements and has only the upper triangle of the symmetric matrix. Each line of the file contains 3 numbers: the row number, the column number and the value in that location of the matrix.

Write mass matrix to file saves the mass matrix with the same two format options as the stiffness matrix.

Write load vector to file saves the global load vector to a file with the value at each DOF on a separate line. If the model contains load cases, the load vectors for each load case are on the same lines separated by commas.

Write DOF reordering to file saves the relationship between global DOF numbers and the row numbers of the matrix. This is only useful in analysis types that use the eigenvalue solver: modal vibration, modal response, acoustic and buckling. A node's global DOF number can be calculated from (node number - 1) × DOFs per node + node DOF number. For example, in the Modal Vibration 3D Solid and Truss analysis type there are 3 DOFs per node so the global DOF for displacement in Y on node 5 would be (5-1)×3+2=14. Each line of the file contains the matrix row number corresponding to the global DOF of that line. Where the global DOF has been condensed out of the matrix, the file shows 0 for the matrix row number.

Samples and Verification

11.1 BeamBendingAndTwisting.liml

Analysis type: Static 3D

Elements: Beam (line2)

Loads and constraints: Fixed support, Force, Moment

This sample shows LISA finding the longitudinal stresses due to bending of a beam using a predefined cross-section. It also shows torsional stiffness and that torsion does not influence longitudinal stress. The beam is made from a hollow rectangular tube with properties:

Width: a=23mm Height: b=50mm

Wall thickness: t=2mm

Length: I=2m

Young's modulus: E=200GPa

Poisson's ratio: 0.3



The beam is oriented at 45 degrees to the Y axis and is fully constrained at one end and loaded at the other end with a lateral force of 1N and a twisting moment of 2Nm.

LISA reports stress at 5 locations on the cross-section: each of the four outer corners and a user defined point p on an inside corner. These results are compared to hand calculations below.

The longitudinal stress at the base of the beam at point 1 (W_1 = 12.5mm) should be

$$\sigma_1 = \frac{M_V W_1}{I_{VV}} = 0.844490 \, MPa$$

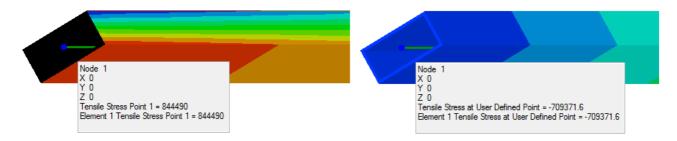
The longitudinal stress at the user defined point p ($W_p = -10.5$ mm) should be

$$\sigma_p = \frac{M_V W_p}{I_{VV}} = -0.709372 \, MPa$$

The bending moment about the V axis (M_V) is $2m \times 1N = 2Nm$. The 2nd moment of area about the V axis (I_{VV}) can be found using a readily available formula and the parallel axis theorem:

$$I_{VV} = 29603 \frac{2}{3} mm^4$$

LISA shows the same stress values:



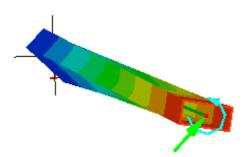
The twisting angle can be found using

$$\theta = \frac{l T}{GJ}$$

where I is the beam length (2m), T is the applied torque (2Nm), G is the modulus of rigidity $(\frac{200}{2.6} GPa)$, and J is the torsion constant which is approximated by [3]

$$J \approx \frac{2t (a-t)^2 (b-t)^2}{a+b-2t} = 6.86657 \times 10^{-8} m^4$$

This gives θ =7.5729×10⁻⁴ radians which is the same as the twist angle found by LISA because LISA uses the same approximate formula for J.



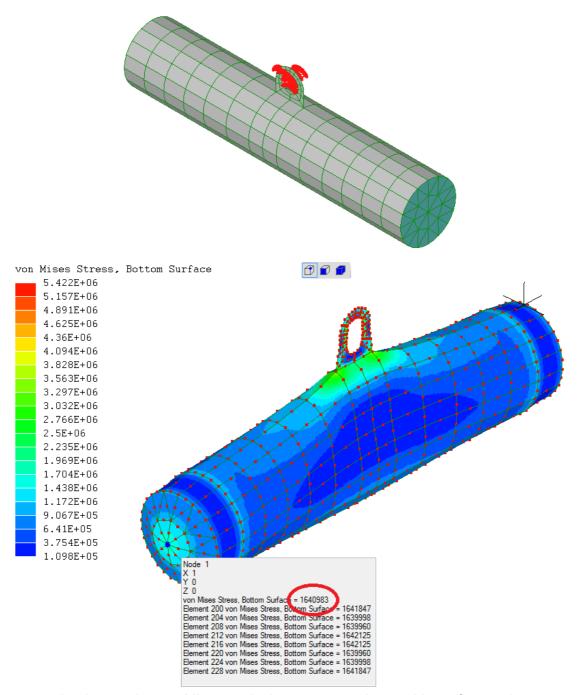
11.2 CylinderLifting.liml

Analysis type: Static 3D

Elements: Shell (tri6, quad8)

Loads and constraints: Fixed support, Gravity, Pressure, Load cases

This sample shows the use of shell elements for a pressure vessel in two different load cases – self weight under gravity, and the same with an additional internal pressure load. It also uses material of different thickness for the end caps.



In the pressure load case, the von Mises equivalent stress on the outside surface at the center of each end cap is 1.64×106Pa. Mesh refinement to 16 times the number of elements shows this stress to be in error by about 2%. The outside surface is called the bottom surface in the solution. You can see this by turning on **Show element axes** to show the direction of the blue W axis of each element.

11.3 PressureVesselAxisymmetric.liml

Analysis type: Static axisymmetric

Elements: Axisymmetric continuum (quad8)

Loads and constraints: Displacement, Pressure

This is a cylindrical pressure vessel with semi-ellipsoidal ends. It is modeled as axi-symmetric because the geometry and loads all have axial symmetry about the longitudinal axis. Only one half is modeled due to mirror symmetry and a displacement constraint in the Y direction is applied to enforce this boundary condition.

It is made from steel (E=200GPa, ν =0.3) with wall thickness t=20mm, inside radius r=500mm and internal pressure P=1MPa.

Three tests are used to validate the results:

The longitudinal reaction force in the cylindrical wall at the mirror symmetry boundary is

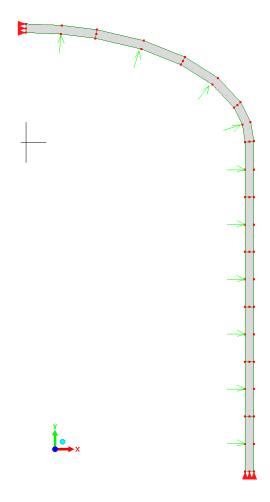
$$F_Y = -P \times \pi r^2 = -785 \text{kN}$$
 compared to LISA's -798 kN

The axial stress in the cylindrical wall is

$$\sigma_{yy} = \frac{F_y}{\pi((r+t)^2 - r^2)} = 12.25 \text{MPa}$$
 compared to LISA's 12.44 MPa

The hoop stress in the middle of the cylindrical wall is

$$\sigma_{ZZ} = \frac{Pr}{t} = 25.00 \text{MPa}$$
 compared to LISA's 25.00 Mpa



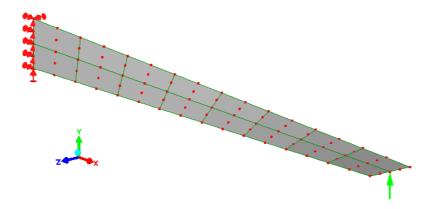
11.4 TwistedBeam.liml

Analysis type: Static 3D

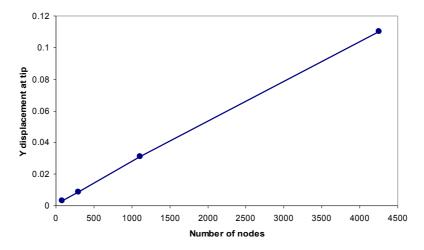
Elements: Shell (quad9)

Loads and constraints: Fixed support, Force

This sample demonstrates a popular test case where LISA's shell elements fail to produce results because they are warped. It is a cantilever beam with a 90° twist along its length and a point load at the free end.



The graph below shows that as the mesh is refined, the displacement at the tip increases in proportion to the number of nodes. It does not converge to a solution. The first data point with 85 nodes is the solution from the sample pictured above without any mesh refinement.



Failure to converge with mesh refinement

11.5 BucklingBeam.liml

Analysis type: Buckling 2D Beam

Elements: Beam (line2)

Loads and constraints: Fixed Support, Force

Consider a column fixed at the base and free at the top, subject to an axial compressive force. We will find the value of the force at which it buckles, the critical load.

The column is of length L=100mm, the cross section is a 10mm×10mm square and the Young's modulus is E=200,000 N/mm².

The model is made with line2 elements. The bottom face has a fixed support to constrain displacement and rotation. A point load of 1N has been applied at the top.

The Euler buckling equation is used to calculate the critical load:

$$P_{cr} = \pi^2 E I / (K L)^2$$

K = 2 for these boundary conditions

 $E = 2 \times 10^5 \text{N/m}^2$

I = 833.333mm⁴

L = 100 mm

Critical load, Pcr= 41123N

The buckling factor for mode 1 found by LISA is 41125 and approaches the theoretical value with mesh refinement. This is equal to the buckling load in newtons because a force of 1N was applied in the model. The mode shape shows that this is indeed the first buckling mode.

The shift point is set to 1000 which is typically reasonable being an order of magnitude below the lowest buckling factor.

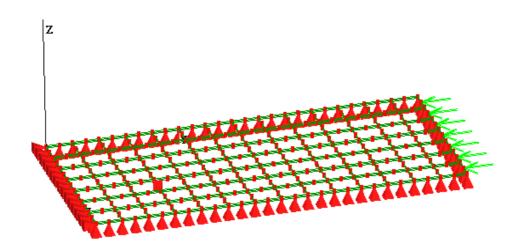
11.6 BucklingPlate.liml

Analysis type: Buckling 3D Solid and Truss

Elements: Solid continuum (hex20)

Loads and constraints: Displacement, Pressure

Consider a simply supported plate with compressive edge loading on two opposite edges. We will determine the critical loads of lowest few buckling modes.



The translational motions along the Z axis are constrained for all the edges, but they are free to rotate about the edge directions. Translational motion in the X-Y plane is allowed, except the bottom edge is restrained to provide a reaction to the applied force. A single arbitrarily chosen node is constrained in the x direction to prevent rigid body motion.

The total applied load is equal to 1, so the buckling factors produced by the solver are equal to the critical loads.

For thin plates such as the one used above, the following analytical equation can be used to calculate the first four critical loads:

$$F_{cr} = b\pi^2 a^2 D ([m/a]^2 + [n/b]^2)^2 / m^2$$

F_{cr}: The critical load applied to one edge

a=2: Length in direction of load

b=1: Width

D=E $t^3/[12(1-v^2)]$: Plate rigidity

t=0.0125 : Thickness v=0.3: Poisson's ratio E=1e6: Young's modulus

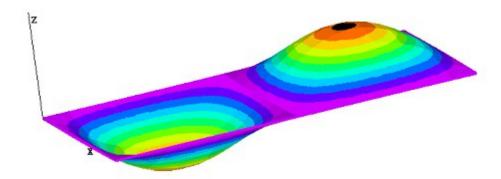
m: Number of half-waves of the buckle in the direction of the load n: Number of half-waves of the buckle perpendicular to the load

For m=1 and n=1, F_{cr}=11.0. The LISA model gives 11.1

For m=2 and n=1, F_{cr}=7.06. The LISA model gives 7.11 (pictured below)

For m=3 and n=1, F_{cr} =8.29. The LISA model gives 8.46 For m=4 and n=1, F_{cr} =11.0. The LISA model gives 11.6

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Notice that the lowest critical load is for the mode with 2 half-waves so this mode will develop first under increasing load.

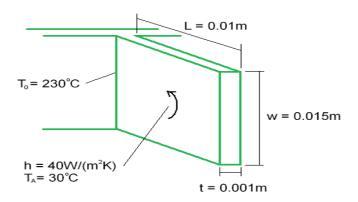
11.7 FinConvection.liml

Analysis type: Thermal Steady State

Elements: Fin (line2, line3)

Loads and constraints: Temperature, Convection

LISA will find the temperature distribution along the length of the thermal fin shown below. Heat enters the base of the fin which is held at a fixed temperature of 230°C and is lost through the 4 sides by convection. The material has thermal conductivity of k=380W/(mK). The model contains two alternative meshes for the same fin, one using a line3 element and the other using two line2 elements.



The temperature (Tx) a distance x from the base of the fin is given by

$$\frac{T_x - T_a}{T_0 - T_a} = \frac{\cosh(mL - mx)}{\cosh(mL)}$$

where
$$m = \sqrt{\frac{hP}{kA}}$$

P is the perimeter of the cross-section, 0.032m

A is the area of the cross-section, 0.000015m²

The table below shows close agreement between LISA's results and the temperatures given by the above formula.

Location	T _x from the formula	2×line2 elements	1×line3 element
Midpoint (x=0.005m)	228.3306°C	228.3299°C	228.3306°C
End (x=0.01m)	227.7752°C	227.7742°C	228.7752°C

11.8 ConductionConvectionRadiation.liml

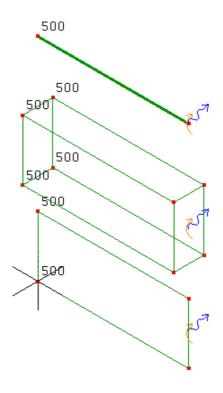
Analysis type: Thermal Steady State

Elements: Shell (quad4), Solid continuum (hex8), fin (line2)

Loads and constraints: Temperature, Convection, Radiation

This model shows one-dimensional steady state heat transfer by conduction, convection and radiation through a slab of thickness 0.05 m. Heat flows in through the left hand surface which is held at 500 K and heat flows out through the right hand surface by both convection (heat transfer coefficient h = 37.5 $W/(m^2K)$) and radiation (emissivity $\epsilon = 0.8$) to an ambient temperature of 300 K.

Three versions of the model are included in the same file, using shell, solid and fin elements. All three give the same results except heat flux is not available for the fin element.



To verify the analysis we will perform a simple heat balance:

$$q_{conduction} = q_{convection} + q_{radiation}$$

Heat flux by conduction $(q_{\text{conduction}})$ is given by LISA as the x component of heat flux which is the same over the entire model

$$q_{conduction} = 3591.65 \text{ W/m}^2$$

Heat flux by convection is found using the temperature LISA calculated for the right hand face $(T_{\text{surface}}=380.2783\text{K})$

$$q_{convection} = h(T_{surface} - T_{ambient}) = 3010.44 \text{ W/m}^2$$

Heat flux by radiation is found in a similar way but using the Stefan-Boltzmann law

$$q_{radiation} = \epsilon \sigma (T_{surface}^4 - T_{ambient}^4) = 581.21 \text{ W/m}^2$$

where σ is the Stefan-Boltzmann constant, 5.67037/10⁻⁸ Wm⁻²K⁻⁴

The heat balance equation is satisfied:

$$3591.65 \text{ W/m}^2 = 3010.44 \text{ W/m}^2 + 581.21 \text{ W/m}^2$$

11.9 OscillatingHeatFlow.liml

Analysis type: Thermal Transient

Elements: Shell (quad8)

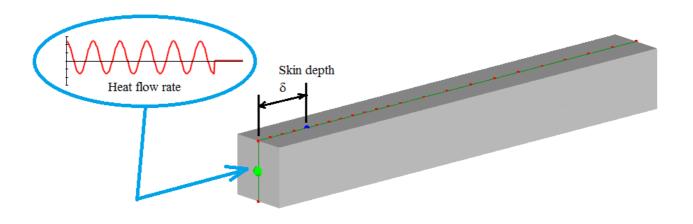
Loads and constraints: Heat flow rate

An insulated aluminum bar is heated by an oscillating thermal load applied to one end then removed. LISA will find the temperature in the bar as a function of both time and distance along the bar. The material properties are:

Specific heat capacity, cp = 900 K/(kg.K)

Density, $\rho = 2700 \text{ kg/m}3$

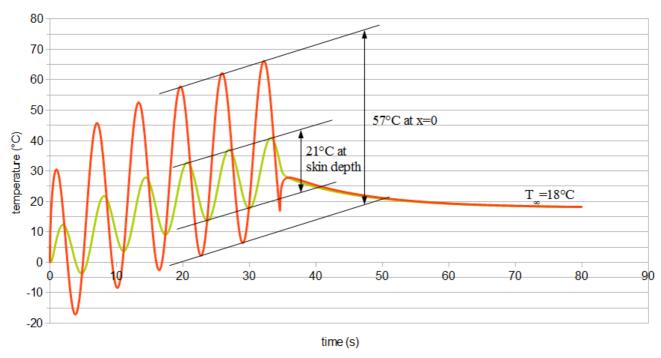
Thermal conductivity, k = 200 W/(m.K)



The heat load Q(t) is input into LISA as a table of heat flow rate values every 0.2s according to this function:

$$Q(t) = \begin{cases} (100\cos(t) + 20)W & t \le 34.6s \\ 0 & t > 34.6s \end{cases}$$

The graph below shows the temperature variation with time at two points. The red curve is measured at the end of the bar (x=0) and the green curve is temperature measured at the skin depth $(x=\delta)$.



These results are verified in two ways, first by comparing the ratio of the temperature wave amplitudes at two points to their theoretical ratio, and second by comparing the net heat input to the total temperature rise after it has reached equilibrium.

The skin depth δ is the distance at which the amplitude of the temperature variation is 1/e of the amplitude at x=0. It is given by

$$\delta = \sqrt{\frac{kP}{\rho c_p \pi}}$$

where P is the period of the temperature wave. $P=2\pi$

$$\delta = 0.01283001$$
m

A mesh node is located at $x=\delta$ for convenient measurement. The graph above shows the peak-peak amplitude of temperature at this node is 21°C. It also shows the peak-peak amplitude of temperature at x=0 is 57°C. $57/20 = 2.85 \approx e$ as required.

The expected temperature rise from t=0 to t=∞ is

$$\Delta T = \frac{Q_{net}}{\rho c_n V}$$

 $V = volume of the bar = 1.5625 \times 10^{-5} m^3$

$$Q_{net} = \int_{0}^{34.6} Q(t)dt$$

$$= \int_{0}^{34.6} (100\cos(t) + 20) W dt$$

$$= [100\sin(t) + 20t]_{a}^{b} J$$

$$= 687.75 J$$

$$\Delta T = 18 \, ^{\circ}C$$

This agrees with the final value of temperature given by LISA across the whole bar which is also 18°C.

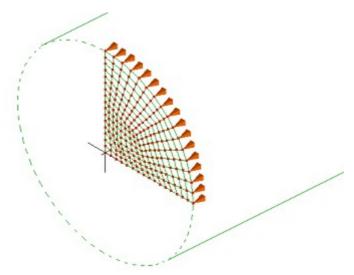
11.10 FluidPipeXSection.liml

Analysis type: Fluid Non-Newtonian Conduit Cross-Section

Elements: Plane continuum (quad4)

Loads and constraints: Pressure Gradient Z, velz

This sample will determine the velocity distribution of a Newtonian fluid flowing in a circular pipe. The pressure gradient of 2000Pa over a pipe length of 1m is 2000 Pa/m. Only one segment of the pipe is modelled due to symmetry. At the outer edge the velocity is constrained to zero representing a no-slip condition.



The theoretical velocity distribution is given by

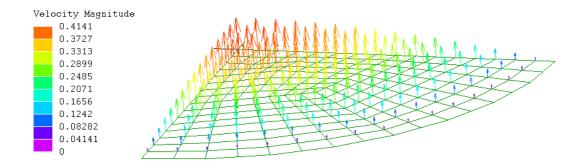
$$V(x) = dP/dZ \times (x^2 - r^2) / (4 \mu)$$

x is the distance from the center of the pipe dP/dZ is the pressure gradient, -2000Pa/m r is the radius of the pipe, 0.1m

 μ is the dynamic viscosity of the fluid, 12 Pa.s

The table below shows the agreement between LISA's results and the formula.

Theoretical velocity	LISA
0.417 m/s	0.414 m/s
0.391 m/s	0.388 m/s
0.313 m/s	0.310 m/s
0.182 m/s	0.180 m/s
0 m/s	0 m/s
	0.417 m/s 0.391 m/s 0.313 m/s 0.182 m/s



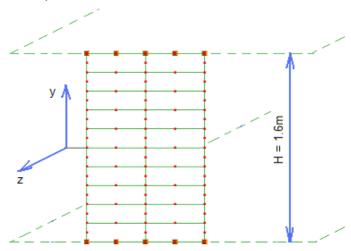
11.11 FluidPseudoplastic.liml

Analysis type: Fluid Non-Newtonian Conduit Cross-Section

Elements: Plane continuum (quad8)

Loads and constraints: Pressure Gradient Z, velz

The velocity distribution in a pseudo-plastic fluid flowing between infinite parallel plates will be found by a hand calculation and compared to LISA's results



The theoretical velocity profile is given by the following equation [5]

$$V_{z}(y) = \phi \left(-\frac{dP}{dz}\right)^{\frac{1}{n}} \frac{\left(\frac{H}{2}\right)^{\frac{1}{n}+1} - y^{\frac{1}{n}+1}}{\frac{1}{n}+1}$$

dP/dZ: pressure gradient = -10Pa/m

n = 0.7

 $\phi: K = \phi^{-n} = 1$

H: gap width = 1.6m

y: vertical distance from the center of the gap

Y-coordinate	Theoretical velocity	LISA
0 m	6.425 m/s	6.394 m/s
0.16 m	6.296 m/s	6.278 m/s
0.32 m	5.731 m/s	5.719 m/s
0.48 m	4.567 m/s	4.559 m/s
0.64 m	2.688 m/s	2.685 m/s
0.80 m	0.000 m/s	0.000 m/s

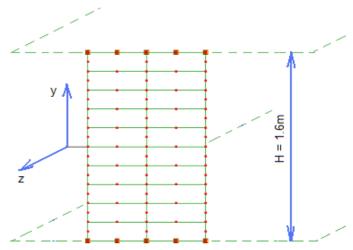
11.12 FluidBingham.liml

Analysis type: Fluid Non-Newtonian Conduit Cross-Section

Elements: Plane continuum (quad8)

Loads and constraints: Pressure Gradient Z, velz

The velocity distribution will be found for a Bingham fluid flowing between parallel plates.



The fluid forms a solid plug in the middle of the channel where the shear stress is less than τ_0 . The expected velocity of this plug is 1.4 × average velocity and the half-width of the plug is [6]

$$h_p = \tau_0/|dP/dZ|$$

dP/dZ: pressure gradient = -10Pa/m

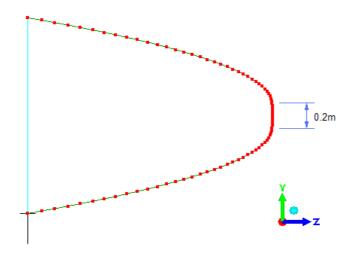
 τ_0 : critical shear stress = 1 Pa

H: gap width = 1.6m

K = 1

n = 1

The solution shows a plug velocity of 2.45m/s which is $1.43 \times 1.43 \times$



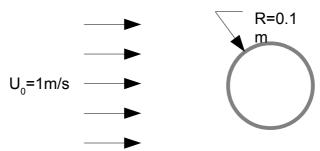
11.13 FluidPotentialCylinder.liml

Analysis type: Potential Flow 2D

Elements: Plane continuum (tri3, quad4)

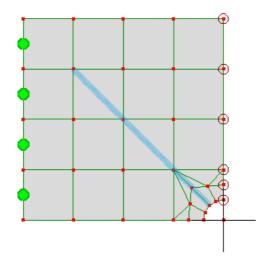
Loads and constraints: Flow rate, velocitypotential

LISA will be used to analyze the flow of water (ρ =1000kg/m³) around a cylinder of radius R=0.1m. The flow is assumed to be incompressible, inviscid and irrotational.



The mesh is made of only one quadrant by taking advantage of symmetry. Velocity potential is set to zero along the midplane of the cylinder because this plane will be perpendicular to the flow direction. A

flow rate of 3m3/s is applied to the 3m2 inlet surface to give a uniform velocity of U0=1m/s over the surface.



The table below compares the solution values with theoretical formulas along the θ =45° line shown in blue in the above picture.

	Velocity potential φ (m²/s)		Velocity magnitude U (m/s)		Dynamic pressure (Pa)	
Radius r	$U_0(r+\frac{R^2}{r})\cos(\theta)$	LISA	$\sqrt{U_0 + \frac{R^4}{r^4}}$	LISA	$\frac{\rho U^2}{2}$	LISA
0.1000	0.141	0.131	1.414	1.404	1000	988
0.2268	0.192	0.189	1.019	1.048	519	555
0.3536	0.270	0.271	1.003	1.037	503	541
0.7071	0.510	0.513	1.000	1.012	500	512
1.0607	0.757	0.762	1.000	1.006	500	506

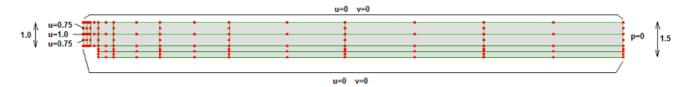
11.14 FluidStep.liml

Analysis type: Fluid Navier-Stokes Equations 2D

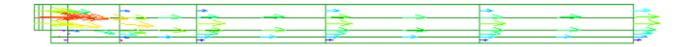
Elements: Plane continuum (quad8)

Loads and constraints: velx, vely, nodepressure

Flow of viscous fluid over a backward facing step is analyzed. Dynamic viscosity = 0.00457, and density=1.0.



The velocity results match those published in [1] including those derived from experiment. An eddy is visible immediately downstream of the step.



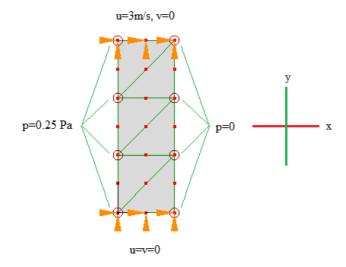
11.15 FluidCouette.liml

Analysis type: Fluid Navier-Stokes Equations 2D

Elements: Plane continuum (tri6)

Loads and constraints: velx, vely, nodepressure

Here an analysis is done for fully developed flow between parallel plates with the lower plate fixed and the upper plate moving parallel to it with a constant velocity U=3m/s. The flow is driven both by the plate movement and an applied pressure gradient of -0.25Pa/m. This kind of flow is commonly known as Couette flow.



The theoretical velocity profile is parabolic, which can be represented exactly by the quadratic tri6 elements so the x-components of velocity from LISA are identical to the theoretical values found from [1]:

$$u(y) = \frac{U}{h} \left(y + \frac{h}{2} \right) - \frac{1}{2u} \frac{\partial p}{\partial x} \left(\frac{h^2}{4} - y^2 \right)$$

where

U = u(1.5) = 3m/s
h = height = 3m

$$\mu$$
 = dynamic viscosity = 0.1 Pa.s
 $\frac{\partial p}{\partial x}$ = pressure gradient = -0.25Pa/m

y (m)	u(y) from formula (m/s)	u(y) from LISA (m/s)
-1.5	0	0
-0.5	3.5	3.5
0	4.3125	4.3125
0.5	4.5	4.5
1.5	3	3

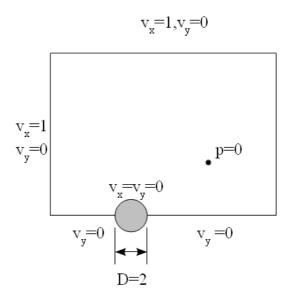
11.16 FluidViscousCylinder.liml

Analysis type: Fluid Navier-Stokes Equations 2D

Elements: Plane continuum (quad8)

Loads and constraints: velx, vely, nodepressure, startvelx, startvely

Rotational laminar flow around a cylinder is analyzed. This example has been taken from [1]. Dynamic viscosity = 0.1 and density = 1. The Reynolds number is 20 which is expected to lead to the boundary layer separating into two steady, symmetrical eddies downstream of the cylinder. Only one will appear in the solution because only one half of the cylinder is modeled.



At the upper and left boundary, the fluid velocity in x (velx) is set to 1 and the fluid velocity in y is zero to represent uniform flow a large distance from the cylinder. At the lower boundary, the y component of velocity (vely) is set to zero to enforce symmetry. On the surface of the cylinder, both components of velocity are zero because it has a no-slip boundary condition.

Start velocities which are close to the final values have been specified to speed up the solution. These are not required for this problem and it will converge to within about 1% of the same solution without them.

The table below shows the close agreement between LISA's results and those published in Taylor and Hughes [1]:

Node number	Source	velocity x	velocity y	pressure
236	Taylor & Hughes	0.404	0.000	0.00173
	LISA	0.404	0.000	0.00173
237	Taylor & Hughes	0.414	-0.0101	-
	LISA	0.414	-0.0101	-
238	Taylor & Hughes	0.442	-0.0187	0.00211
	LISA	0.442	-0.0187	0.00211
243	Taylor & Hughes	1.12	-0.0215	-
	LISA	1.12	-0.0215	-
244	Taylor & Hughes	1.08	-0.0159	-0.0113
	LISA	1.08	-0.0159	-0.0113

11.17 VibratingFreePlate.liml

Analysis type: Modal Vibration 3D Shell and Beam

Elements: Shell (quad8)

Loads and constraints: none

This sample shows the undamped natural vibration modes of a square plate without any supports. Its properties are:

Side length, a = 0.1m

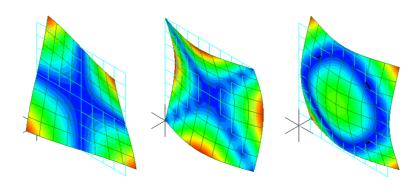
Thickness, h = 1mm

Young's modulus E = 200 GPa

Poisson's ratio, v = 0.225

Density, $\rho = 8000 \text{ kg/m}^3$

The first three deformation modes found by LISA are shown below along with their angular frequencies. LISA also produces 6 rigid body modes because the plate is unconstrained.



 ω_1 = 2114 rad/s

 $\omega_2 = 3122 \text{ rad/s}$

 $\omega_3 = 3662 \text{ rad/s}$

These results are verified by comparison with analytical formulas [7]:

$$\omega = \frac{\alpha}{a^2} \sqrt{\frac{D}{\rho h}}$$

$$D = \frac{Eh^3}{12(1-v^2)}$$

 $\alpha_1 = 14.10$, $\omega_1 = 2089$ rad/s

 α_2 = 20.56, ω_2 = 3046 rad/s

 α_3 = 23.91, ω_3 = 3542 rad/s

For all three modes the error is less than 4% and can be reduced to less than 1% with mesh refinement.

11.18 VibratingCantileverBeam.liml

Analysis type: Modal Vibration 3D Shell and Beam

Elements: Beam (line2)

Loads and constraints: Fixed support

Beam elements are used to model a vibrating cantilever fixed at one end and free at the other. Four elements are needed to capture the higher bending modes. The beam's properties are:

Length, L = 2.4m

Width, b = 0.1m

Height, h = 0.05m

Young's modulus, E = 200 GPa

Density, $\rho = 7860 \text{ kg/m}^3$







The frequencies of the first 3 modes for bending in the XY plane are verified by the formula

$$f_n = \frac{\alpha^2}{2\pi} \sqrt{\frac{EI}{\rho bhL^4}}$$

$$\alpha_1 = 1.875$$

$$\alpha_2 = 4.694$$

$$\alpha_3 = 7.885$$

$$I = \frac{bh^3}{12} = 2.0833 \times 10^{-6} m^4$$

which gives these frequencies compared to LISA

Mode	Frequency from formula	Frequency from LISA
n=1	7.073 Hz	7.074 Hz
n=2	44.33 Hz	44.38 Hz
n=3	125.1 Hz	125.1 Hz

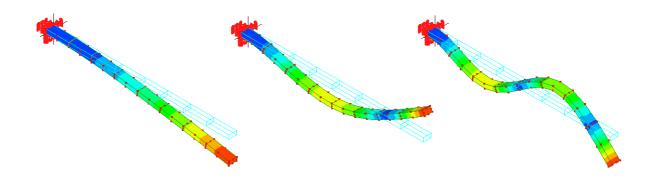
11.19 VibratingCantileverSolid.liml

Analysis type: Modal Vibration 3D Solid and Truss

Elements: Solid continuum (hex20)

Loads and constraints: Fixed support

This is a model of the same beam described in VibratingCantileverBeam.liml but it is made using hex20 solid elements. The picture below shows the same mode shapes that are shown for VibratingCantileverBeam.liml.



Mode	Frequency from formula	Frequency from LISA
n=1	7.073 Hz	7.089 Hz
n=2	44.33 Hz	44.99 Hz
n=3	125.1 Hz	128.7 Hz

11.20 VibratingTrussTower.liml

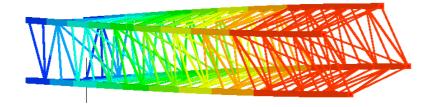
Analysis type: Modal Vibration 3D Solid and Truss, Static 3D

Elements: Truss (line2)

Loads and constraints: Displacement, Force

A truss tower will be analyzed to find the fundamental torsional vibration mode. It is 20m high and made from 10 identical 1m×1m×2m sections connected end to end. Each section uses two types of steel beam – the chords at the corners have $0.01m^2$ cross sectional area and the bracing members have $0.001m^2$ cross sections. All joints are free to rotate in any direction. The steel's Young's modulus is 200GPa and density is $7800kg/m^3$. The 4 nodes at the base are constrained against displacement in all directions.

The first two modes found by LISA are bending modes and the 3rd is the fundamental torsion mode shown below with frequency



This result is validated using the formula for the fundamental torsion mode of a uniform shaft with distributed mass

$$f = \frac{1}{4} \sqrt{\frac{K}{I}}$$

I = 3640.54 kgm² is the rotational inertia of the whole structure about it's longitudinal axis. It can be found by summing the rotational inertia of all 250 truss elements.

K is the torsional stiffness of the structure. This is found by using LISA to perform a static analysis with an applied torque of 1Nm then measuring the resulting rotation at the end. The torque is applied using 4 forces on the top 4 nodes. If you change the analysis type to Static 3D then solve it, it will show the top nodes each rotate by $\theta = 2.92843 \times 10^{-7}$ radians about the longitudinal axis of the tower. This gives $K = 1Nm / \theta = 3.41480 \times 10^6$ Nm/radian.

The frequency given by this formula matches LISA's result to within 0.3%.

$$f = 7.66 Hz$$

11.21 VibratingMembrane.liml

Analysis type: Modal Vibration 2D Transverse Vibration of Membrane

Elements: Plane continuum (tri3)

Loads and constraints: Fixed Support, Tension per Length

A hexagonal sheet of fabric is fixed around its outer edge and held in a state of uniform isotropic biaxial tension. It can vibrate like a drum head due to the stiffness caused by its tension. We will find its first 3 natural frequencies and mode shapes.

Density: 1000kg/m³ Thickness: 1mm

Distance between opposite corners: 600mm

Tension per unit length: 2N/m

The results shown below closely match the results from the sample VibratingMembraneCyclicSymmetry.liml which is the same problem analyzed using solid elements.

Mode	Mode shape	Frequency
1, 0 nodal diameters		2.033 Hz
3, 1 nodal diameter. Mode 2 is a similar mode with the same frequency but a different orientation.		3.304 Hz
4, 2 nodal diameters. Mode 5 is a similar mode with the same frequency but a different orientation.		4.539 Hz

11.22 VibratingMembraneCyclicSymmetry.liml

Analysis type: Modal Vibration 3D Solid and Truss

Elements: Solid continuum (wedge6)

Loads and constraints: Fixed Support, Thermal Stress, Temperature, Cyclic

Symmetry, Stress Stiffening

This is the same structure as the sample VibratingMembrane.liml but it is modeled using solid elements with stress stiffening and cyclic symmetry.

A hexagonal sheet of fabric is fixed around its outer edge and held in a state of uniform isotropic biaxial tension. It can vibrate like a drum head due to the stiffness caused by its tension. We will find its first 3 natural frequencies and mode shapes.

The uniform stress is applied using thermal strain. An artificial thermal expansion coefficient of 1K⁻¹ is used with an arbitrary small Young's modulus of 0.001N/m² and a temperature change of -2×10⁶K. This generates a stress of 2000N/m² in the plane of the membrane. You can confirm this stress by changing the analysis type to Static 3D and solving.

Because the hexagonal shape has 6 identical segments, only one segment is modeled and cyclic symmetry is used to represent the others. LISA will find modes which are cyclically symmetric as well as those that aren't. The table below shows close agreement with the results from the sample VibratingMembrane.liml.

Mode	Mode shape	Frequency
1, 0 nodal diameters. Mode 2 is a spurious mode caused by the artificially low stiffness of the material.		2.033 Hz
4, 1 nodal diameter. Mode 3 is a spurious mode caused by the artificially low stiffness of the material.		3.304 Hz
6, 2 nodal diameters. Mode 5 is a spurious mode caused by the artificially low stiffness of the material.		4.539 Hz

11.23 VibratingString.liml

Analysis type: Modal Vibration 3D

Elements: Solid continuum (hex8)

Loads and constraints: Displacement, Stress Stiffening, Force

We will model the transverse vibration of a straight flexible cable held in tension. The cable has the following properties:

• Length: L=60m

Linear density: ρ=3kg/m

• Tensile force: F=40N

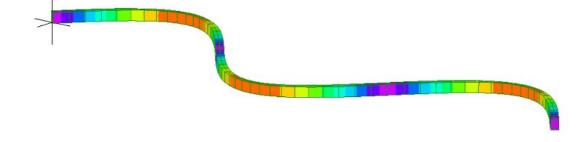
• Bending stiffness: Negligible

The solution is compared to hand calculation using the formula

$$f = n/2 (F/\rho)^{1/2}/L$$

where f is the frequency and n is the mode number of the standing wave. The LISA model includes axial modes which are ignored here because they are a consequence of the arbitrary material stiffness.

Mode	f (hand calculation)	f (LISA)
n=1	0.03043 Hz	0.03042 Hz
n=2	0.06086 Hz	0.06088 Hz
n=3	0.09129 Hz	0.09141 Hz
n=4	0.1217 Hz	0.1221 Hz



11.24 PandSWaves.liml

Analysis type: Dynamic Response 2D

Elements: Plane continuum (quad4)

Loads and constraints: Displacement, Force

Dynamic response analysis is used to model wave propagation through an elastic medium (rock). A sinusoidal force is applied at the center of an infinite domain. This generates pressure waves (P-waves) traveling outward in the direction of the force, and shear waves (S-waves) traveling outward perpendicular to the force.

Only one quadrant of the domain is modeled due to symmetry. The symmetry is enforced by constraining displacement in Y along the axes of symmetry. LISA has no infinite boundary condition so a finite boundary far from the source of the waves is used instead. The analysis is only run until the first waves reach the boundary so any reflections from the boundary are excluded.

The material's properties are:

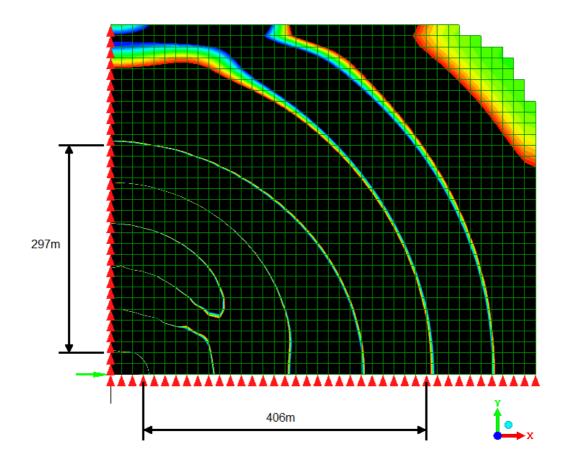
Young's modulus E = 7 GPa

Poisson's ratio v = 0.2

Density ρ = 3000 kg/m³

Shear modulus
$$G = \frac{E}{2(1+v)} = 2.917 \, GPa$$

Bulk modulus
$$K = \frac{E}{3(1-2v)} = 3.889 GPa$$



The contour plot above at time = 0.4s shows locations of zero displacement in the X direction as colored lines. This type of display is convenient for measuring wavelengths of waves of different amplitudes. It was generated by setting the **User defined maximum and minimum** to 1e12 an -1e12 respectively.

The solution is verified by comparing the wavelengths of the P-waves and S-waves to their theoretical values.

The tape measure tool is used to measure the average wavelength of two P-waves along the X axis as 406m/2 = 203m. In the same way, the average wavelength of 2.5 S-waves measured along the Y axis is 297m/2.5 = 119m.

The theoretical wavelengths are

$$\lambda_p = \frac{c_p}{f}$$
 and $\lambda_s = \frac{c_s}{f}$

where

$$f = \frac{50}{2\pi} Hz \quad \text{is the frequency of the applied force}$$

$$c_p = \sqrt{\frac{\frac{4}{3}G + K}{\rho}} = 1610 \, m/s \quad \text{is the speed of P-waves}.$$

$$c_s = \sqrt{\frac{G}{\rho}} = 986.0 \, m/s$$
 is the speed of S-waves.

This gives

$$\lambda_p = 202 \, m$$
 and $\lambda_s = 124 \, \mathrm{m}$

which is within 5% of LISA's results of 203m and 119m respectively.

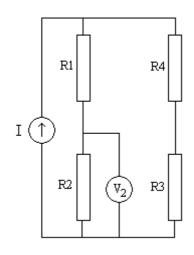
11.25 WheatstoneBridge.liml

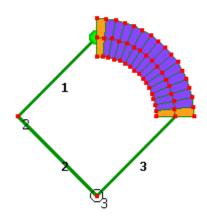
Analysis type: DC Current Flow

Elements: Resistor (line2), Solid continuum (hex8)

Loads and constraints: Voltage, Current

The Wheatstone bridge circuit shown below is modeled in LISA to find the voltage V₂ across R2 with an applied current of I=100mA. Three of the resistors are line2 resistor elements and R4 is modeled using solid elements having high-conductivity terminals to connect to the resistor elements. Node 3 is constrained to 0V and is the reference point for voltages at the other nodes.





 $R1=750\Omega$

 $R2=1000\Omega$

 $R3 = 500\Omega$

R4=1169.826 Ω which was found by integration of the curved shape.

Hand calculation shows that the voltage at node 2 is

$$V_2 = I \frac{(RI + R2)(R3 + R4)}{RI + R2 + R3 + R4} \frac{R2}{RI + R2} = 48.828V$$

which matches LISA's result of 48.823V. Most of the error is due to coarseness of the solid element mesh of R4 and can be eliminated by replacing it with a line2 resistor element having the resistance listed above.

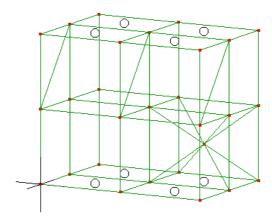
11.26 Capacitor.liml

Analysis type: Electrostatic 3D

Elements: Solid continuum (pyr5, wedge6, hex8)

Loads and constraints: Voltage

The electric field between two plates of a capacitor will be modeled. The plates are d=0.25m apart with a dielectric (ϵ_r =2.5) in-between and a potential difference of V=1.5V across them. Each plate has an area of A=0.2m×0.3m.



The expected electric field is

$$E = V / d$$

= 1.5V / 0.25m = 6 V/m

which is consistent with the results from LISA of 6.000000 V/m on each node.

The expected energy stored in the capacitor is

$$U = 1/2 \text{ C V}^2$$
$$= 5.9766 \times 10^{-12} \text{ J}$$

where

$$C = A \epsilon_r \epsilon_0 / d$$

 $\varepsilon_0 = 8.854187818 \times 10^{-12} \text{ F/m}$, the permittivity of free space

This corresponds to an energy density of $U \times A \times d = 3.9844 \times 10^{-10} \text{ J/m}^3$. The energy density given by LISA is also $3.9844 \times 10^{-10} \text{ J/m}^3$.

Edge effects do not appear in this model because the mesh has no elements outside the area between the plates.

11.27 MagnetWire.liml

Analysis type: Magnetostatic 2D

Elements: Plane continuum (quad4)

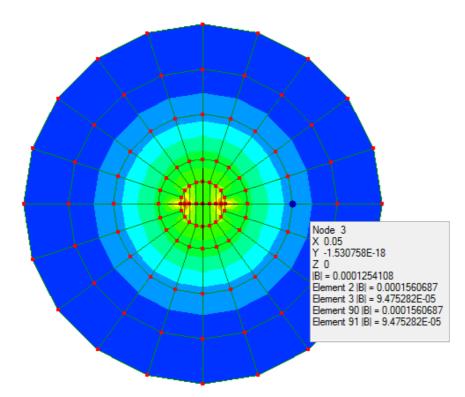
Loads and constraints: Current, Magnetic vector potential

This model is a single infinitely long wire perpendicular to the x-y plane, with a current of I=30A flowing in the +Z direction and surrounded by empty space with a relative permeability of μ_r =1.

The magnitude of the magnetic field at a distance r from the center of an isolated wire is given by

$$|B| = \mu_0 I/(2\pi r)$$

At r=0.05m this gives |B|=0.120mT compared to LISA's solution of 0.125mT. LISA also shows the field being circular and directed counter-clockwise.



Automation and Batch Processing

12.1 Command Line Parameters

Command line parameters can be used to run LISA from another application, batch file or shell script.

```
lisa8 [<filename> [solve]]
```

The optional <filename> is a file of any of the mesh or geometry types that LISA can open. It causes LISA to start with that file open. The file name must include the extension such as .liml, .stp, etc. For example:

```
lisa8 mymodel.liml
```

If you specify a file name then the optional **solve** parameter causes LISA to solve the file then exit without displaying the main window. To obtain the solution, set an output file in the model, such as **Write solution to liml file** or a table with **Write to csv file after solving**. When you use the **solve** parameter, <filename> can contain wildcards. For example to solve all liml files in the current folder, run:

```
lisa8 *.liml solve
```

12.2 COM Interface

LISA's COM interface enables you to write programs which can call a limited range of functions inside LISA to automate some tasks. You can do this using the VBA scripting language included in Microsoft Excel.

Before you use the COM interface for the first time, you must register it. Registration creates registry keys in Windows that help other applications identify LISA and its type library. It only applies to the user running LISA so other users of the same computer will also have to register it before they use the COM interface. Select **COM registration** from the **Options** sub-menu of the **Tools** menu then click **Register** then **Close**.

A single class, lisa8.LisaCode is exposed through COM. Below is a list of all its public members:

12.2.1 General

Property	NumberOfModes()	Gets or sets the number of modes for modal vibration.	Int32
Sub	Open (String FileName)	Opens the specified file.	
Sub	Import(String FileName)	Opens the specified file and combines it with the currently loaded model.	

Sub	SaveAs(String FileName)	Saves to the specified file.	
Sub	PostProc()	Shows the post processor window.	
Sub	PreProc()	Shows the modeler window.	
Sub	Solve()	Solves the currently loaded model.	
Function	Version()	Returns the version number of LISA .	String

12.2.2 Meshing

Function	AddNode(Double X, Double Y, Double Z)	Creates a new node at the specified coordinates. Returns its node number.	Int32
Function	AddElement(Shape Shape, N1, N2, N20)	Creates a new element with the specified nodes. Returns its element number.	Int32
Function	AddElement8(Shape Shape, N1, N2, N8)	Creates a new element with the specified nodes. Returns its element number.	Int32
Property	ElementNode(Int32 ElemID, Int32 LocalNode)	Gets or sets the global node number of the specified local node in an element.	Int32
Function	ElementNumberOfNodes (Int32 ElemID)	Gets the number of nodes in the specified element	Int32
Function	NumberOfElements()	Gets the number of elements in the model.	Int32
Function	NumberOfNodes()	Gets the number of nodes in the model.	Int32
Property	X(Int32 NodeID)	Gets or sets a node's X coordinate.	Double
Property	Y(Int32 NodeID)	Gets or sets a node's Y coordinate.	Double
Property	Z (Int32 NodeID)	Gets or sets a node's Z coordinate.	Double
Enumeration	Shape	Element shapes. To use this, the type library (LISA 8 FEA Type Library) must be added to the client's reference list.	Int32

12.2.3 Post-processing

Function	AngularFrequency(Int32 Mode)	Gets the frequency of a vibration mode from the solution.	Double
Enumeration	FieldValue	Identifies solution field values with friendly names. To use this, the type library (LISA 8 FEA Type Library) must be added to the client's reference list.	Int32
Function	NodeValue(Int32 NodeID, FieldValue FieldValue, Int32 StepNo)	Gets the solution value at a node. StepNo is either load case, time step or mode number depending on what is present in the solution.	Double

FEA Math

13.1 Variational Principle

Physical laws of science are usually expressed as differential equations of rates of change. As the finite element method uses the computational ability of a microprocessor, the differential equation form is not immediately suitable for the finite element method. Thus, the problem has to be reformulated as a Variational Principle. The Variational Principle works with energy instead. For example, in Statics, the variational form of the problem uses the principle of minimum energy which states that : at equilibrium, the extension is such that the potential energy is a minimum.

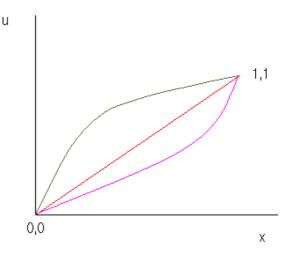
The potential energy of an element in statics may consist of i. strain energy and ii. gravitational energy. The total energy V(u(x)), in the structure is given by an expression integrating the strain and gravitational energies over the entire structure. Where u(x) is the nodal displacement which is a function of distance, x (here, one-dimensional analysis) and the potential energy V is a function of the nodal displacement, u.

Thus the finite element analysis problem is to find the nodal displacement u(x) which minimizes the energy V(u(x)), yet satisfies the boundary constraints for u(x) [example u(0) = 0 and u(1) = b]. V(u(x)) is called a functional and u(x) a function. The relation between the function and functional may best be expressed by:

"given a distance, x, the nodal displacement function "u" determines a corresponding number u(x)" "given a function, u, the functional V determines a corresponding number V(u(x))".

13.2 Explaining the Functional V(u(x))

Consider geometrically the various functions of u(x) that satisfy the boundary conditions, at x=0, u=0 and at x=1, u=1 as shown above (here only three of the infinite number of u(x) functions that satisfy the boundary conditions have been shown). Any of these u(x) functions when substituted into the functional V(u(x)) give the potential energy of the structure.



13.3 Shape Functions

An assumption has to made about how the extension u(x) varies over each element. The simplest assumption is that it varies linearly, however it can vary parabolically or according to other higher order polynomials. Instead of specifying u(x) as an equation in x, an elegant and useful form of specifying u(x) is in the form of a Shape Function. For example in a one dimensional element with two nodes, i and j, the shape functions

Ni(x) and Nj(x) may be specified as : Ni(X)

Ni(x) = 1 at x = xi and = 0 at x=xj

Nj(x) = 0 at x = xi and = 1 at x = xj

Graphically the linear one dimensional shape functions look like

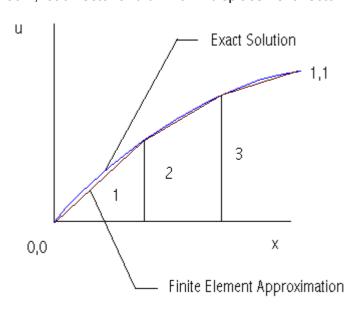
Therefore u(x) = Ni(x)Ui + Nj(x)Uj

this.

Where Ui and Uj are the one-dimensional nodal displacements of the element nodes i and j. Thus, this expression for u(x) is substituted in the energy equation of V(u(x)).

13.4 Minimizing the Functional V(u(x))

The finite element method finds the optimum nodal displacements Ui and Uj (one dimensional element with nodes i and j) by differentiating the functional V(u(x)) with respect to the nodal degrees of freedom Ui and Uj to find stationary points. A system of simultaneous equations is obtained with the nodal displacements of each element as the unknowns. These equations are represented as a stiffness matrix, load vector and unknown displacement vector.



As shown, the one dimensional model has been discretized using 3 elements. The FE method finds the optimum nodal displacements such that the element nodes i,j of the all three elements approach the actual true u(x) exact solution.

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14.5 OCC CAD Kernel

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